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Chapter - 9: Some Applications of Trigonometry

Exercise 9.1 (Page 203 of Grade 10 NCERT)

Q1. A circus artist is climbing a 20 m long rope, which is tightly stretched and tied from the top of a vertical pole to the ground. Find the height of the pole, if the angle made by the rope with the ground level is 30° (see Fig. 9.11).

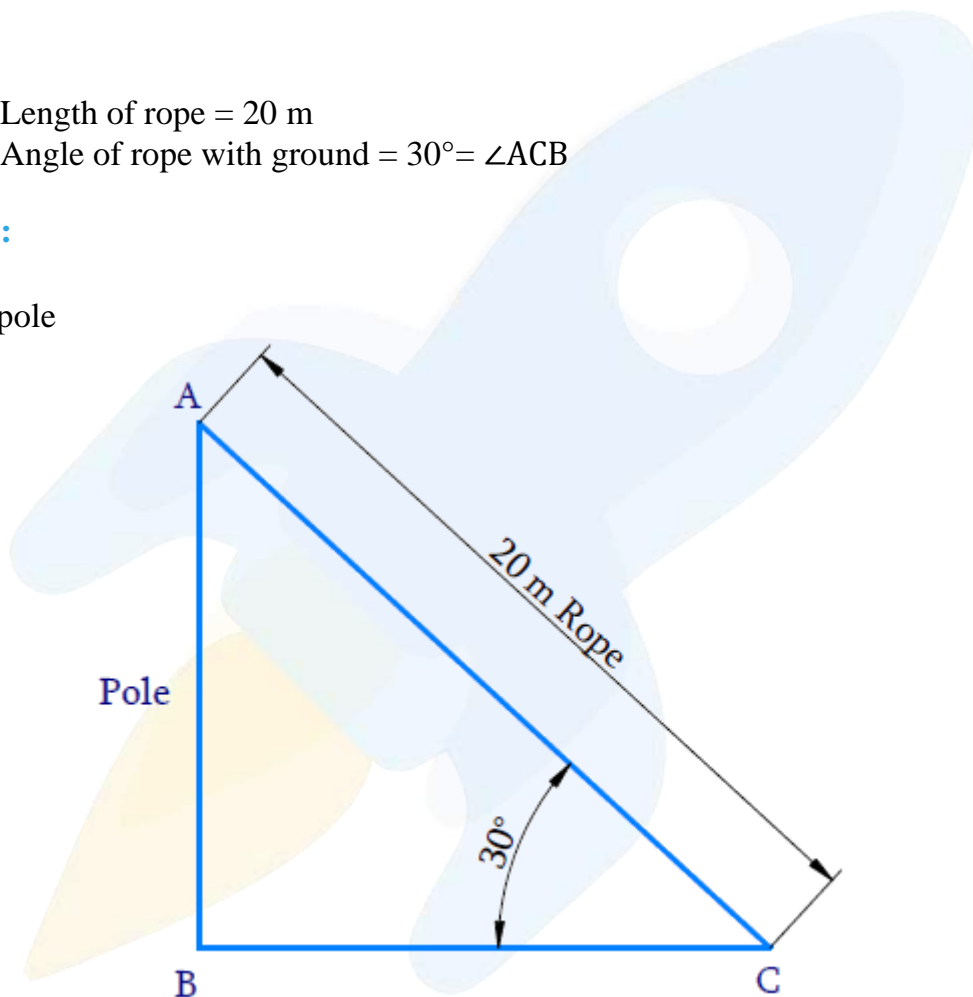
Difficulty Level: Easy

Known:

- (i) Length of rope = 20 m
- (ii) Angle of rope with ground = $30^\circ = \angle ACB$

Unknown:

Height of pole



Reasoning:

AB = Height of the Pole

BC = Distance between the point on the ground and the pole.

AC = Length of the Rope (Hypotenuse)

We need to find the height of the pole AB, from the angle C and the length of the rope AC. Therefore, Trigonometric ratio involving all the three measures is $\sin C$.

In $\triangle ABC$,

$$\sin C = \frac{AB}{AC}$$

$$\sin 30^\circ = \frac{AB}{20}$$

$$\frac{1}{2} = \frac{AB}{20}$$

$$AB = \frac{1}{2} \times 20$$

$$AB = 10 \text{ m}$$

Answer:

Height of pole $AB = 10 \text{ m}$

Q2. A tree breaks due to storm and the broken part bends so that the top of the tree touches the ground making an angle 30° with it. The distance between the foot of the tree to the point where the top touches the ground is 8 m. Find the height of the tree.

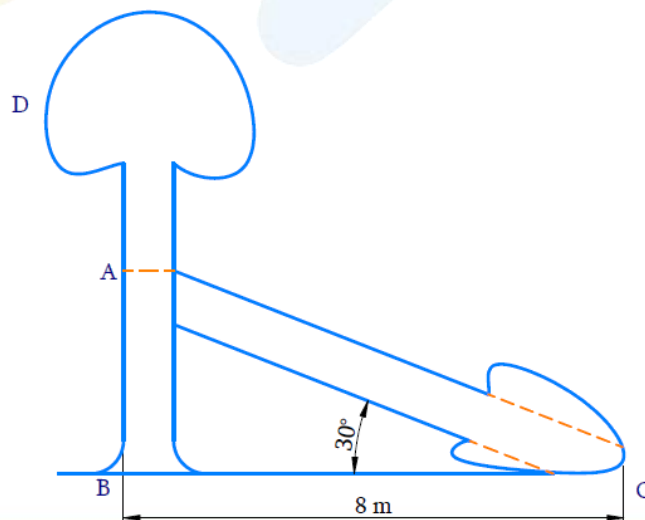
Difficulty Level: Medium

Unknown:

Height of the tree

Known:

- (i) Broken part of the tree bends and touching the ground making an angle of 30° with the ground.
- (ii) Distance between foot of the tree to the top of the tree is 8 m



Reasoning:

- (i) Height of the tree = $AB + AC$
- (ii) Trigonometric ratio which involves AB , BC and $\angle C$ is $\tan \theta$, where AB can be measured.
- (iii) Trigonometric ratio which involves AB , AC and $\angle C$ is $\sin \theta$, where AC can be measured.
- (iv) Distance between the foot of the tree to the point where the top touches the ground = $BC = 8$ m

Solution:In $\triangle ABC$,

$$\tan C = \frac{AB}{BC}$$

$$\tan 30^\circ = \frac{AB}{8}$$

$$\frac{1}{\sqrt{3}} = \frac{AB}{8}$$

$$AB = \frac{8}{\sqrt{3}}$$

$$\sin C = \frac{AB}{AC}$$

$$\sin 30^\circ = \left(\frac{\frac{8}{\sqrt{3}}}{AC} \right)$$

$$\frac{1}{2} = \frac{8}{\sqrt{3}} \times \frac{1}{AC}$$

$$AC = \frac{8}{\sqrt{3}} \times 2$$

$$AC = \frac{16}{\sqrt{3}}$$

$$\text{Height of tree} = AB + AC$$

$$= \frac{8}{\sqrt{3}} + \frac{16}{\sqrt{3}}$$

$$= \frac{24}{\sqrt{3}}$$

$$= \frac{24}{\sqrt{3}} \times \frac{\sqrt{3}}{\sqrt{3}}$$

$$= \frac{24\sqrt{3}}{3}$$

$$= 8\sqrt{3}$$

Answer: Height of tree = $8\sqrt{3}$ m

Q3. A contractor plans to install two slides for the children to play in a park. For the children below the age of 5 years, she prefers to have a slide whose top is at a height of 1.5 m and is inclined at an angle of 30° to the ground, whereas for elder children she wants to have a steep slide at a height of 3m and inclined at an angle of 60° to the ground. What should be the length of the slide in each case?

Difficulty Level: Medium

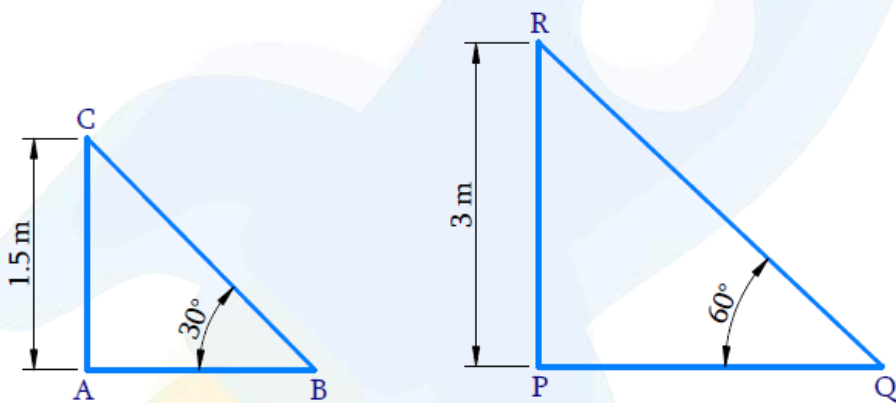
Unknown:

Length of the slide for children below the age of 5 years and elder children.

Known:

(i) For the children below the age of 5 years.

Height of the slide = 1.5m
Slide's angle with the ground = 30°



(ii) For elder children.

Height of the slide = 3m
Slide's angle with the ground = 60°

Reasoning:

Let us consider the following conventions for the slide installed for children below 5 years:

- The height of the slide as AC.
- Distance between the foot of the slide to the point where it touches the ground as AB.
- Length of the slide as BC

Let us consider the following conventions for the slide installed for elder children:

- The height of the slide PR.
- Distance between the foot of the slide to the point where it touches the ground as PQ.
- Length of the slide as QR.

- (i) Trigonometric ratio involving AC, BC and $\angle B$ is $\sin \theta$
- (ii) Trigonometric ratio involving PR, QR and $\angle Q$ is $\sin \theta$

Solution:

- (i) In $\triangle ABC$,

$$\sin 30^\circ = \frac{AC}{BC}$$

$$\frac{1}{2} = \frac{1.5}{BC}$$

$$BC = 1.5 \times 2$$

$$BC = 3$$

- (ii) In $\triangle PRQ$,

$$\sin Q = \frac{PR}{QR}$$

$$\sin 60^\circ = \frac{3}{QR}$$

$$\frac{\sqrt{3}}{2} = \frac{3}{QR}$$

$$QR = \frac{3 \times 2}{\sqrt{3}}$$

$$= \frac{6}{\sqrt{3}} \times \frac{\sqrt{3}}{\sqrt{3}}$$

$$= \frac{6\sqrt{3}}{3}$$

$$= 2\sqrt{3}$$

Answer:

Length of slide for children below 5 years = 3 m

Length of slide for elder children = $2\sqrt{3}$ m

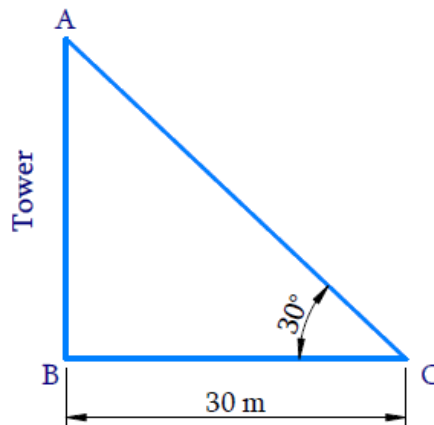
Q4. The angle of elevation of the top of a tower from a point on the ground, which is 30 m away from the foot of the tower, is 30° . Find the height of the tower.

Difficulty Level: Medium**Known:**

- (i) Angle of elevation of the top of the tower from a point on ground is 30°
- (ii) Distance between the foot of the tower to the point on the ground is 30 m.

Unknown:

Height of the tower

**Reasoning:**

Let us consider the height of the tower as AB, distance between the foot of tower to the point on ground as BC.

In $\triangle ABC$,

Trigonometric ratio involving AB, BC and $\angle C$ is $\tan \theta$.

Solution:

In $\triangle ABC$,

$$\begin{aligned}\tan C &= \frac{AB}{BC} \\ \tan 30^\circ &= \frac{AB}{30} \\ \frac{1}{\sqrt{3}} &= \frac{AB}{30} \\ AB &= \frac{30}{\sqrt{3}} \\ &= \frac{30}{\sqrt{3}} \times \frac{\sqrt{3}}{\sqrt{3}} \\ &= \frac{30\sqrt{3}}{3} \\ &= 10\sqrt{3}\end{aligned}$$

Answer:

Height of tower $AB = 10\sqrt{3} \text{ m}$

Q5. A kite is flying at a height of 60 m above the ground. The string attached to the kite is temporarily tied to a point on the ground. The inclination of the string with the ground is 60° . Find the length of the string, assuming that there is no slack in the string.

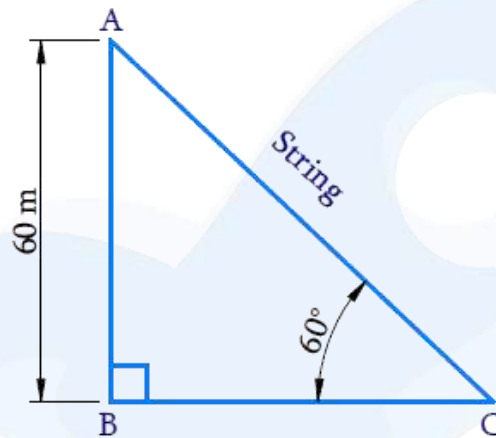
Difficulty Level: Medium

Known:

- (i) Height of the flying kite = 60m
- (ii) Angle made by the string to the ground = 60°

Unknown:

Length of the string



Reasoning:

Let the height of the flying kite as AB, length of the string as AC and the inclination of the string with the ground as $\angle C$.

Trigonometric ratio involving AB, AC and $\angle C$ is $\sin \theta$

Solution:

In $\triangle ABC$,

$$\begin{aligned}\sin C &= \frac{AB}{AC} \\ \sin 60^\circ &= \frac{60}{AC} \\ \frac{\sqrt{3}}{2} &= \frac{60}{AC} \\ AC &= \frac{60 \times 2}{\sqrt{3}} \\ &= \frac{120}{\sqrt{3}} \times \frac{\sqrt{3}}{\sqrt{3}} \\ &= \frac{120\sqrt{3}}{3} \\ &= 40\sqrt{3}\end{aligned}$$

Answer:

Length of the string $AC = 40\sqrt{3} m$

Q6. A 1.5 m tall boy is standing at some distance from a 30 m tall building. The angle of elevation from his eyes to the top of the building increases from 30° to 60° as he walks towards the building. Find the distance he walked towards the building.

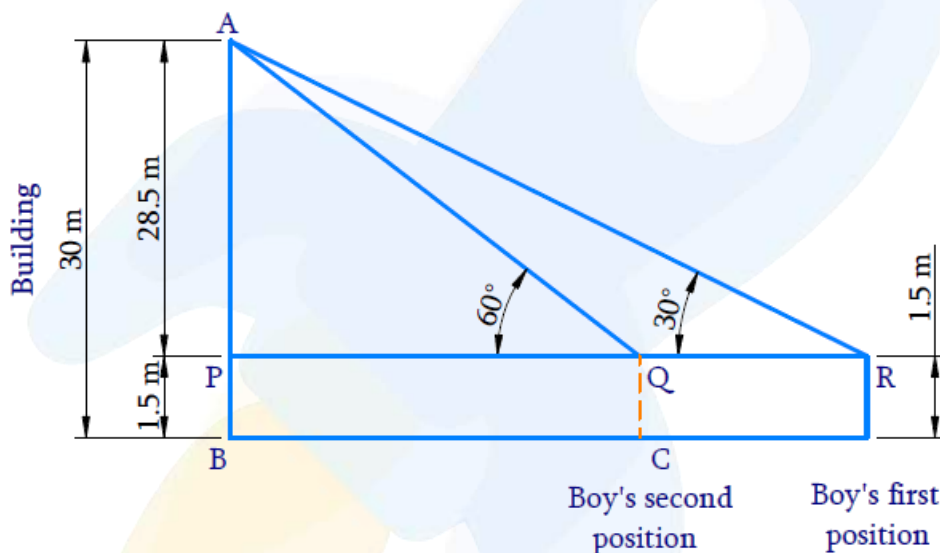
Difficulty Level: Hard

Known:

- (i) Height of the boy = 1.5 m
- (ii) Height of the building = 30 m
- (iii) Angle of elevation from his eyes to the top of the building increases from 30° to 60° as he walks toward the building.

Unknown:

Distance, the boy walked towards the building



Reasoning:

Trigonometric ratio involving $(AP, PR \text{ and } \angle R)$ and $(AP, PQ \text{ and } \angle Q)$ is $\tan \theta$ [Refer the diagram to visualise AP, PR and PQ]

Distance walked towards the building $RQ = PR - PQ$

Solution:In $\triangle APR$

$$\tan R = \frac{AP}{PR}$$

$$\tan 30^\circ = \frac{28.5}{PR}$$

$$\frac{1}{\sqrt{3}} = \frac{28.5}{PR}$$

$$PR = 28.5 \times \sqrt{3} \text{ m}$$

In $\triangle APQ$

$$\tan Q = \frac{AP}{PQ}$$

$$\tan 60^\circ = \frac{28.5}{PQ}$$

$$\sqrt{3} = \frac{28.5}{PQ}$$

$$PQ = \frac{28.5}{\sqrt{3}} \text{ m}$$

Therefore,

$$\begin{aligned} PR - PQ &= 28.5\sqrt{3} - \frac{28.5}{\sqrt{3}} \\ &= 28.5 \left(\sqrt{3} - \frac{1}{\sqrt{3}} \right) \\ &= 28.5 \left(\frac{3-1}{\sqrt{3}} \right) \\ &= 28.5 \left(\frac{2}{\sqrt{3}} \right) \\ &= \frac{57}{\sqrt{3}} \\ &= \frac{57}{\sqrt{3}} \times \frac{\sqrt{3}}{\sqrt{3}} \\ &= \frac{57\sqrt{3}}{3} \\ &= 19\sqrt{3} \text{ m} \end{aligned}$$

Answer:Distance the boy walked towards the building is $19\sqrt{3}$ m

Q7. From a point on the ground, the angles of elevation of the bottom and the top of a transmission tower fixed at the top of a 20 m high building are 45° and 60° respectively. Find the height of the tower.

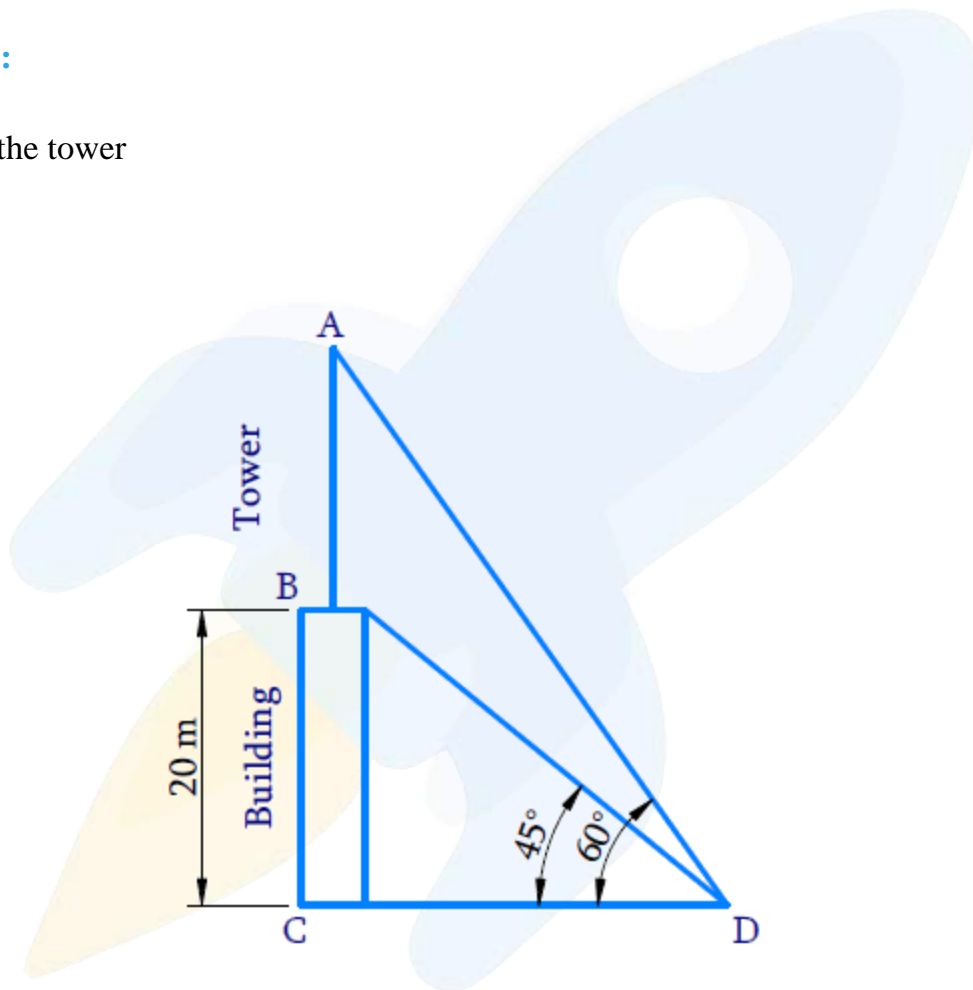
Difficulty Level: Hard

Known:

- (i) Angle of elevation from ground to bottom of the tower = 45°
- (ii) Angle of elevation from ground to top of the tower = 60°
- (iii) Height of the building = 20 m
- (iv) Tower is fixed at the top of the 20 m high building

Unknown:

Height of the tower



Reasoning:

Let the height of the building is BC, height of the transmission tower which is fixed at the top of the building is AB. D is the point on the ground from where the angles of elevation of the bottom B and the top A of the transmission tower AB are 45° and 60° respectively.

The distance of the point of observation D from the base of the building C is CD

Combined height of the building and tower = AC = AB + BC

Trigonometric ratio involving sides AC, BC, CD, and $\angle D$ (45° and 60°) is $\tan \theta$

Solution:

In $\triangle BCD$,

$$\tan 45^\circ = \frac{BC}{CD}$$

$$1 = \frac{20}{CD}$$

$$CD = 20$$

In $\triangle ACD$,

$$\tan 60^\circ = \frac{AC}{CD}$$

$$\sqrt{3} = \frac{AC}{20}$$

$$AC = 20\sqrt{3}$$

Answer:

Height of the tower, $AB = AC - BC$

$$AB = 20\sqrt{3} \text{ m} - 20 \text{ m}$$

$$= 20(\sqrt{3} - 1) \text{ m}$$

Q8. A statue, 1.6 m tall, stands on the top of a pedestal, from a point on the ground. The angle of elevation of the top of the statue is 60° and from the same point the angle of elevation of the top of the pedestal is 45° . Find the height of the pedestal.

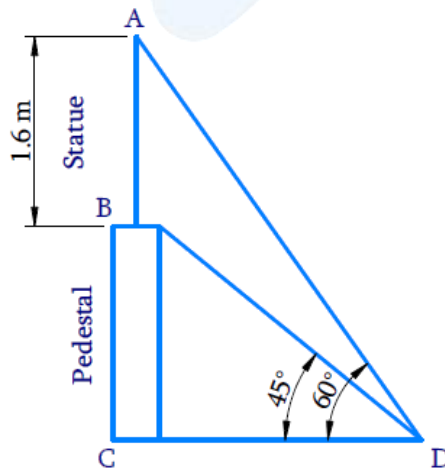
Difficulty Level: Hard

Known:

- (i) Height of statue = 1.6 m
- (ii) Angle of elevation from ground to top of the statue = 60°
- (iii) Statue stands on the top of the pedestal.
- (iv) Angle of elevation of the top of the pedestal (bottom of the statue) = 45°

Unknown:

Height of the pedestal



Reasoning:

Let the height of the pedestal is BC, height of the statue, stands on the top of the pedestal, is AB. D is the point on the ground from where the angles of elevation of the bottom B and the top A of the statue AB are 45° and 60° respectively.

The distance of the point of observation D from the base of the pedestal C is CD

Combined height of the pedestal and statue $AC = AB + BC$

Trigonometric ratio involving sides AC, BC, CD, and $\angle D$ (45° and 60°) is $\tan \theta$

Solution:

In $\triangle BCD$,

$$\begin{aligned}\tan 45^\circ &= \frac{BC}{CD} \\ 1 &= \frac{BC}{CD} \\ BC &= CD \quad \text{(i)}\end{aligned}$$

In $\triangle ACD$,

$$\begin{aligned}\tan 60^\circ &= \frac{AC}{CD} \\ \tan 60^\circ &= \frac{AB+BC}{CD} \\ \sqrt{3} &= \frac{1.6+BC}{BC} \quad \text{[from (i)]} \\ \sqrt{3}BC &= 1.6+BC \\ \sqrt{3}BC - BC &= 1.6 \\ BC(\sqrt{3}-1) &= 1.6 \\ BC &= \frac{1.6}{\sqrt{3}-1} \times \frac{\sqrt{3}+1}{\sqrt{3}+1} \\ &= \frac{1.6(\sqrt{3}+1)}{3-1} \\ &= \frac{1.6(\sqrt{3}+1)}{2} \\ &= 0.8(\sqrt{3}+1)\end{aligned}$$

Answer:

Height of pedestal $BC = 0.8(\sqrt{3}+1)m$

Q9. The angle of elevation of the top of a building from the foot of the tower is 30° and the angle of elevation of the top of the tower from the foot of the building is 60° . If the tower is 50 m high, find the height of the building.

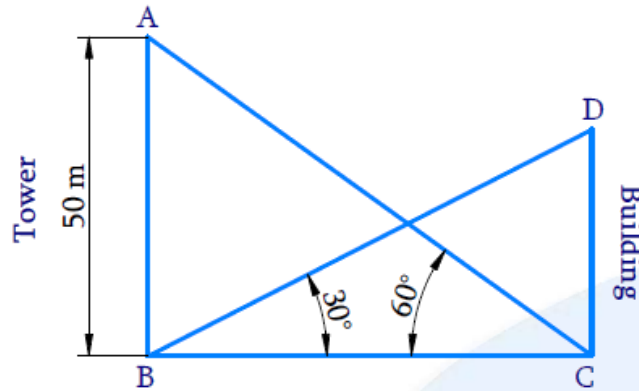
Difficulty Level: Hard

Known:

- (i) Angle of elevation of the top of a building from the foot of the tower = 30°
- (ii) Angle of elevation of the top of the tower from the foot of the building = 60°
- (iii) Height of tower = 50m

Unknown:

Height of the building



Reasoning:

Let the height of the tower is AB and the height of the building is CD. The angle of elevation of the top of the building D from the foot of the tower B is 30° and the angle of elevation of the top of the tower A from the foot of the building C is 60° .

Distance between the foot of the tower and the building is BC.

Trigonometric ratio involving sides AB, CD, BC and angles $\angle B$ and $\angle C$ is $\tan \theta$

Solution:

In $\triangle ABC$,

$$\begin{aligned} \tan 60^\circ &= \frac{AB}{BC} \\ \sqrt{3} &= \frac{50}{BC} \\ BC &= \frac{50}{\sqrt{3}} \quad (i) \end{aligned}$$

In $\triangle BCD$,

$$\begin{aligned} \tan 30^\circ &= \frac{CD}{BC} \\ \frac{1}{\sqrt{3}} &= \frac{CD}{BC} \\ \frac{1}{\sqrt{3}} &= \frac{CD}{50/\sqrt{3}} \quad [\text{from (i)}] \\ CD &= \frac{1}{\sqrt{3}} \times \frac{50}{\sqrt{3}} \\ CD &= \frac{50}{3} \\ CD &= 16\frac{2}{3} \end{aligned}$$

Answer:

Height of the building $CD=16\frac{2}{3}m$

Q10. Two poles of equal heights are standing opposite each other on either side of the road, which is 80 m wide. From a point between them on the road, the angles of elevation of the top of the poles are 60° and 30° respectively. Find the height of the poles and the distances of the point from the poles.

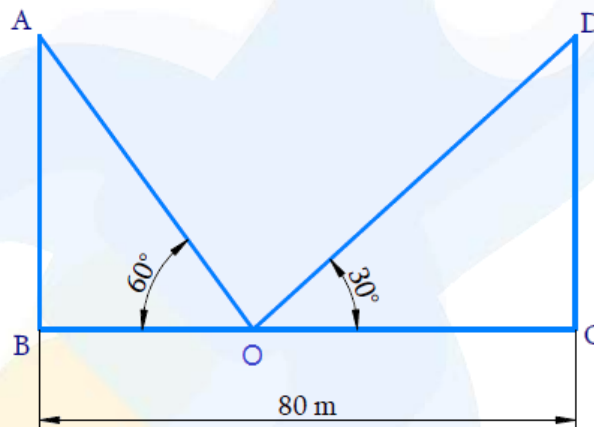
Difficulty Level: Hard

Known:

- (i) The poles of equal height.
- (ii) Distance between poles = 80 m
- (iii) From a point between the poles, the angle of elevation of the top of the poles are 60° and 30° respectively.

Unknown:

Height of the poles and the distances of the point from the poles.



Reasoning:

Let us consider the two poles of equal heights as AB and DC and the distance between the poles as BC. From a point O, between the poles on the road, the angle of elevation of the top of the poles AB and CD are 60° and 30° respectively.

Trigonometric ratio involving angles, distance between poles and heights of poles is $\tan \theta$

Solution:

Let the height of the poles be x

Therefore $AB = DC = x$

In $\triangle AOB$,

$$\tan 60^\circ = \frac{AB}{BO}$$

$$\sqrt{3} = \frac{x}{BO}$$

$$BO = \frac{x}{\sqrt{3}} \quad (i)$$

In $\triangle OCD$,

$$\tan 30^\circ = \frac{DC}{OC}$$

$$\frac{1}{\sqrt{3}} = \frac{x}{BC - BO}$$

$$\frac{1}{\sqrt{3}} = \frac{x}{80 - \frac{x}{\sqrt{3}}} \quad [\text{from (i)}]$$

$$80 - \frac{x}{\sqrt{3}} = \sqrt{3}x$$

$$\frac{x}{\sqrt{3}} + \sqrt{3}x = 80$$

$$x \left(\frac{1}{\sqrt{3}} + \sqrt{3} \right) = 80$$

$$x \left(\frac{1+3}{\sqrt{3}} \right) = 80$$

$$x \left(\frac{4}{\sqrt{3}} \right) = 80$$

$$x = \frac{80\sqrt{3}}{4}$$

$$x = 20\sqrt{3}$$

Height of the poles $x = 20\sqrt{3} \text{ m}$

Distance of the point O from the pole AB

$$BO = \frac{x}{\sqrt{3}}$$

$$= \frac{20\sqrt{3}}{\sqrt{3}}$$

$$= 20$$

Distance of the point O from the pole CD

$$OC = BC - BO$$

$$= 80 - 20$$

$$= 60$$

Answer:

Height of the poles are $20\sqrt{3} \text{ m}$ and the distances of the point from the poles are 20m and 60m .

Q11. A TV tower stands vertically on the bank of a canal. From a point on the other bank directly opposite the tower, the angle of elevation of the top of the tower is 60° . From another point 20 m away from this point on the line joining this point to the foot of the tower, the angle of elevation of the top of the tower is 30° (see Fig. 9.12). Find the height of the tower and the width of the canal.

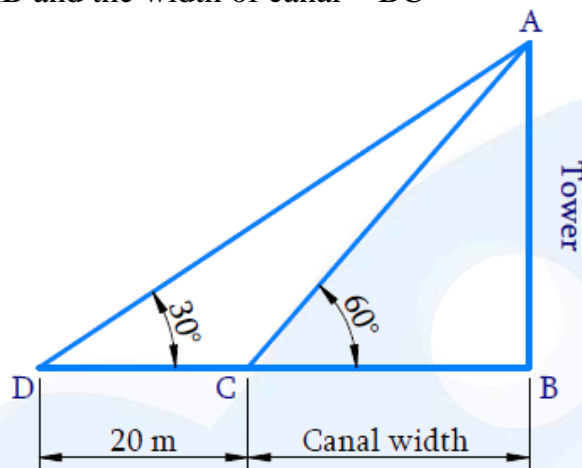
Difficulty Level: Hard

Known:

- (i) The angle of elevation of the top of the tower from a point on the other bank directly opposite the tower is 60°
- (ii) From another point 20 m away from this point in (i) on the line joining this point to the foot of the tower, the angle of elevation of the top of the tower is 30°
- (iii) $CD = 20$ m

Unknown:

Height of the tower = AB and the width of canal = BC



Reasoning:

Trigonometric ratio involving CD, BC, angles and height of tower AB is $\tan \theta$.

Solution:

Considering ΔABC ,

$$\begin{aligned} \tan 60^\circ &= \frac{AB}{BC} \\ \sqrt{3} &= \frac{AB}{BC} \\ AB &= BC\sqrt{3} \dots(1) \end{aligned}$$

Considering ΔABD ,

$$\begin{aligned} \tan 30^\circ &= \frac{AB}{BD} \\ \tan 30^\circ &= \frac{AB}{CD + BC} \\ \frac{1}{\sqrt{3}} &= \frac{BC\sqrt{3}}{20 + BC} && \text{From (1)} \\ 20 + BC &= BC\sqrt{3} \times \sqrt{3} \\ 20 + BC &= 3BC \\ 3BC - BC &= 20 \\ 2BC &= 20 \\ BC &= 10 \end{aligned}$$

Substituting $BC = 10$ m in Equation (1), we get

$$AB = 10\sqrt{3} \text{ m}$$

Answer:

Height of the tower $AB = 10\sqrt{3}$

Width of the canal $BC = 10$ m

Q12. From the top of a 7 m high building, the angle of elevation of the top of a cable tower is 60° and the angle of depression of its foot is 45° . Determine the height of the tower.

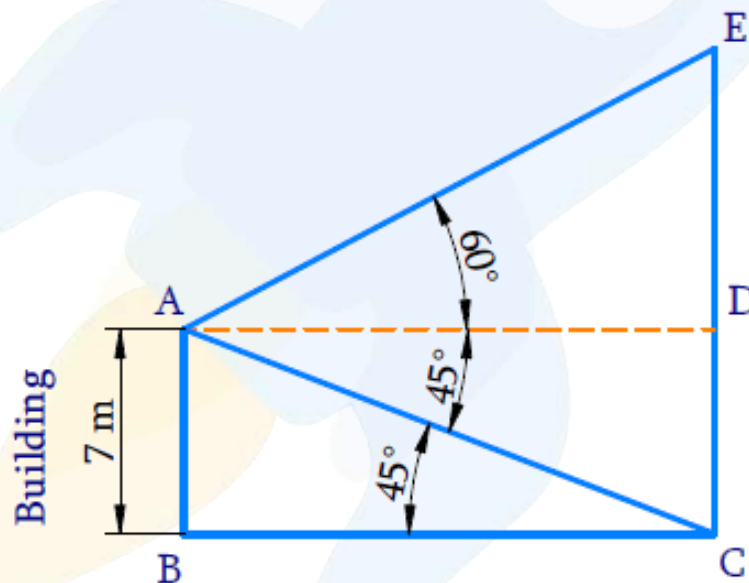
Difficulty Level: Hard

Known:

- (i) Height of building = 7 m
- (ii) Angle of elevation of the top of a cable tower from building top = 60°
- (iii) Angle of depression of the foot of the cable tower from building top = 45°

Unknown:

Height of the tower.



Reasoning:

Let the height of the tower is CE and the height of the building is AB . The angle of elevation of the top E of the tower from the top A of the building is 60° and the angle of depression of the bottom C of the tower from the top A of the building is 45° . Trigonometric ratio involving building height, tower height, angles and distances between them is $\tan \theta$

Solution:

Draw $AD \parallel BC$.

Then, $\angle DAC = \angle ACB = 45^\circ$ (alternate interior angles.)

In $\triangle ABC$,

$$\begin{aligned}\tan 45^\circ &= \frac{AB}{BC} \\ 1 &= \frac{7}{BC} \\ BC &= 7\end{aligned}$$

ABCD is a rectangle,

Therefore, $BC = AD = 7$ and $AB = CD = 7$

In $\triangle ADE$,

$$\begin{aligned}\tan 60^\circ &= \frac{ED}{AD} \\ \sqrt{3} &= \frac{ED}{7} \\ ED &= 7\sqrt{3}\end{aligned}$$

Height of tower

$$\begin{aligned}CE &= ED + CD \\ &= 7\sqrt{3} + 7 \\ &= 7(\sqrt{3} + 1)\end{aligned}$$

Answer:

$$\text{Height of the tower} = 7(\sqrt{3} + 1)m$$

Q13. As observed from the top of a 75 m high lighthouse from the sea-level, the angles of depression of two ships are 30° and 45° . If one ship is exactly behind the other on the same side of the lighthouse, find the distance between the two ships.

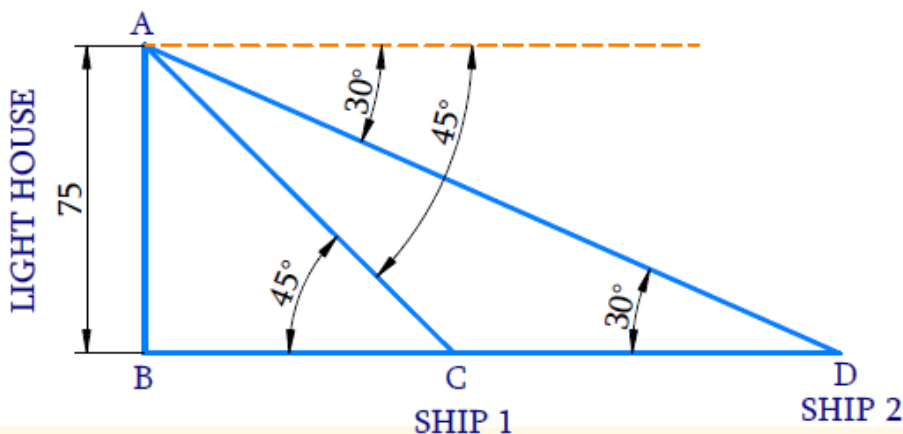
Difficulty Level: Hard

Known:

- (i) Height of the lighthouse = 75 m
- (ii) Angles of depression of two ships from the top of the lighthouse are 30° and 45°

Unknown:

Distance between the two ships



Reasoning:

Let the height of the lighthouse from the sea-level is AB and the ships are C and D . The angles of depression of the ships C and D from the top A of the lighthouse, are 45° and 60° respectively.

Trigonometric ratio involving AB , BC , BD and angles is $\tan \theta$.

Distance between the ships, $CD = BD - BC$

Solution:

In $\triangle ABC$,

$$\tan 45^\circ = \frac{AB}{BC}$$

$$1 = \frac{75}{BC}$$

$$BC = 75$$

In $\triangle ABD$,

$$\tan 30^\circ = \frac{AB}{BD}$$

$$\frac{1}{\sqrt{3}} = \frac{75}{BD}$$

$$BD = 75\sqrt{3}$$

Distance between two ships $CD = BD - BC$

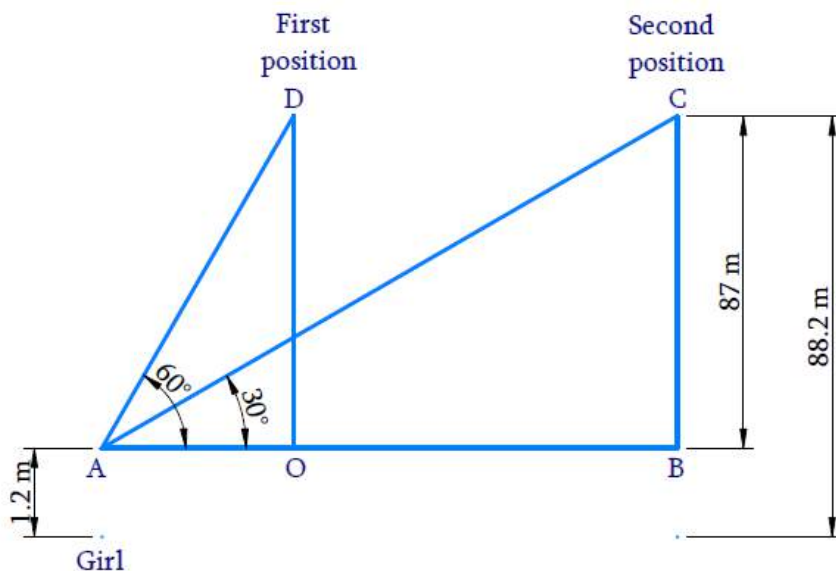
$$CD = 75\sqrt{3} - 75$$

$$= 75(\sqrt{3} - 1)$$

Answer:

Distance between two ships $CD = 75(\sqrt{3} - 1)m$

Q14. A 1.2 m tall girl spots a balloon moving with the wind in a horizontal line at a height of 88.2 m from the ground. The angle of elevation of the balloon from the eyes of the girl at any instant is 60° . After some time, the angle of elevation reduces to 30° (see Fig. 9.13). Find the distance travelled by the balloon during the interval.



Difficulty Level: Hard

Known:

- (i) Height of the girl = 1.2 m
- (ii) Vertical height of balloon from ground = 88.2 m
- (iii) Angle of elevation of the balloon from the eyes of the girl is reducing from 60° to 30° as the balloon moves along wind.
- (iv) From the figure, $OD = BC$ can be calculated as
 $88.2 \text{ m} - 1.2 \text{ m} = 87 \text{ m}$ ----- Result (1)

Unknown:

Distance travelled by the balloon, OB

Reasoning:

Trigonometric ratio involving AB, BC, OD, OA and angles is $\tan \theta$. [Refer AB, BC, OA and OD from the figure.]

Distance travelled by the balloon $OB = AB - OA$

Solution:

From the figure, $OD = BC$, can be calculated as
 $88.2 \text{ m} - 1.2 \text{ m} = 87 \text{ m}$ ----- (1)

In ΔAOD ,

$$\begin{aligned} \tan 60^\circ &= \frac{OD}{OA} \\ \sqrt{3} &= \frac{87}{OA} \\ OA &= \frac{87}{\sqrt{3}} \\ &= \frac{87}{\sqrt{3}} \times \frac{\sqrt{3}}{\sqrt{3}} \\ &= \frac{87 \times \sqrt{3}}{3} \\ &= 29\sqrt{3} \text{m} \end{aligned}$$

In ΔABC ,

$$\begin{aligned} \tan 30^\circ &= \frac{BC}{AB} \\ \frac{1}{\sqrt{3}} &= \frac{87}{AB} \\ AB &= 87\sqrt{3} \end{aligned}$$

Distance travelled by the balloon, $OB = AB - OA$

$$\begin{aligned} OB &= 87\sqrt{3} - 29\sqrt{3} \\ &= 58\sqrt{3} \end{aligned}$$

Answer:

Distance travelled by the balloon = $58\sqrt{3} \text{m}$

Q15. A straight highway leads to the foot of a tower. A man standing at the top of the tower observes a car at an angle of depression of 30° , which is approaching the foot of the tower with a uniform speed. Six seconds later, the angle of depression of the car is found to be 60° . Find the time taken by the car to reach the foot of the tower from this point.

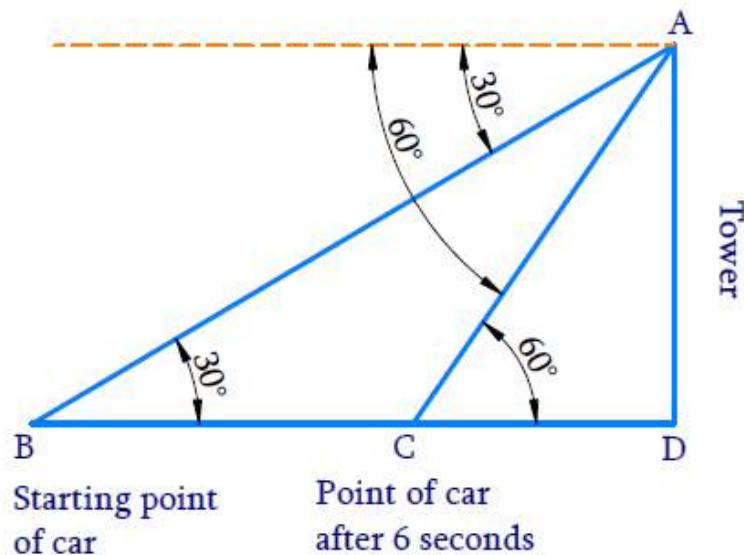
Difficulty Level: Hard

Known:

- (i) Angle of depression is 30°
- (ii) 6 seconds later angle of depression is 60°

Unknown:

Time taken by the car to reach the foot of the tower = CD



Reasoning:

Let the height of the tower as AD and the starting point of the car as B and after 6 seconds point of the car as C. The angles of depression of the car from the top A of the tower at point B and C are 30° and 60° respectively.

Distance travelled by the car from the starting point towards the tower in 6 seconds = BC

Distance travelled by the car after 6 seconds towards the tower = CD

Trigonometric ratio involving AD, BC, CD and angles is $\tan \theta$.

We know that,

$$\text{Speed} = \frac{\text{Distance}}{\text{Time}}$$

The speed of the car is calculated using the distance BC and time = 6 seconds. Using Speed and Distance CD, time to reach foot can be calculated.

Solution:

In $\triangle ABD$,

$$\begin{aligned}\tan 30^\circ &= \frac{AD}{BD} \\ \frac{1}{\sqrt{3}} &= \frac{AD}{BD} \\ BD &= AD\sqrt{3} \dots(1)\end{aligned}$$

In $\triangle ACD$,

$$\begin{aligned}\tan 60^\circ &= \frac{AD}{CD} \\ \sqrt{3} &= \frac{AD}{CD} \\ AD &= CD\sqrt{3} \dots(2)\end{aligned}$$

From equation (1) and (2)

$$\begin{aligned}BD &= CD\sqrt{3} \times \sqrt{3} \\ BC + CD &= 3CD \quad [\because BD = BC + CD] \\ BC &= 2CD \dots(3)\end{aligned}$$

Distance travelled by the car from the starting point towards the tower in 6 seconds = BC
Speed of the car to cover distance BC in 6 seconds;

$$\begin{aligned}\text{Speed} &= \frac{\text{Distance}}{\text{Time}} \\ &= \frac{BC}{6} \\ &= \frac{2CD}{6} \quad [\text{from(3)}] \\ &= \frac{CD}{3}\end{aligned}$$

Speed of the car = $\frac{CD}{3}$ m/s

Distance travelled by the car from point C, towards the tower = CD

Time to cover distance CD at the speed of $\frac{CD}{3}$ m/s

$$\begin{aligned}\text{Time} &= \frac{\text{Distance}}{\text{Speed}} \\ &= \frac{CD}{\frac{CD}{3}} \\ &= CD \times \frac{3}{CD} \\ &= 3\end{aligned}$$

Answer: Time taken by the car to reach the foot of the tower from point C is 3 seconds.

Q16. The angles of elevation of the top of a tower from two points at a distance of 4 m and 9 m from the base of the tower and in the same straight line with it are complementary. Prove that the height of the tower is 6 m.

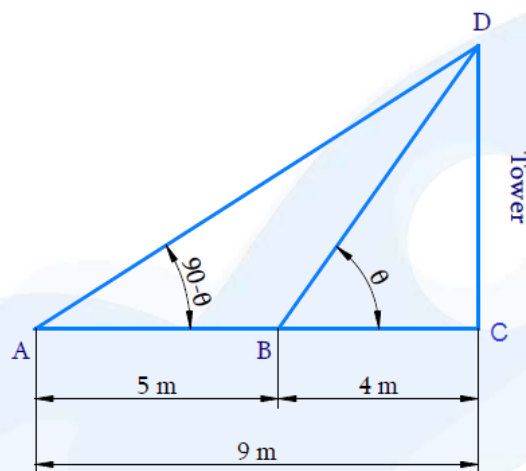
Difficulty Level: Hard

Known:

Angle of elevation of the top of a tower from two points at a distance of 4 m and 9 m from the base of the tower are complimentary.

Unknown:

To prove height of the tower is 6m.



Reasoning:

Let the height of the tower as CD. B is a point 4m away from the base C of the tower and A is a point 5m away from the point B in the same straight line. The angles of elevation of the top D of the tower from the points B and A are complementary.

Since the angles are complementary, if one angle is θ and the other is $(90^\circ - \theta)$.

Trigonometric ratio involving CD, BC, AC and angles is $\tan \theta$.

Using $\tan \theta$ and $\tan(90^\circ - \theta) = \cot \theta$ ratios are equated to find the height of the tower.

Solution:

In $\triangle BCD$,

$$\tan \theta = \frac{CD}{BC}$$

$$\tan \theta = \frac{CD}{4} \quad (1)$$

Here,

$$\begin{aligned} AC &= AB + BC \\ &= 5 + 4 \\ &= 9 \end{aligned}$$

In ΔACD ,

$$\tan(90 - \theta) = \frac{CD}{AC}$$

$$\cot \theta = \frac{CD}{9} \quad \left[\because \tan(90 - \theta) = \cot \theta \right]$$

$$\frac{1}{\tan \theta} = \frac{CD}{9} \quad \left[\because \cot \theta = \frac{1}{\tan \theta} \right]$$

$$\tan \theta = \frac{9}{CD} \quad (2)$$

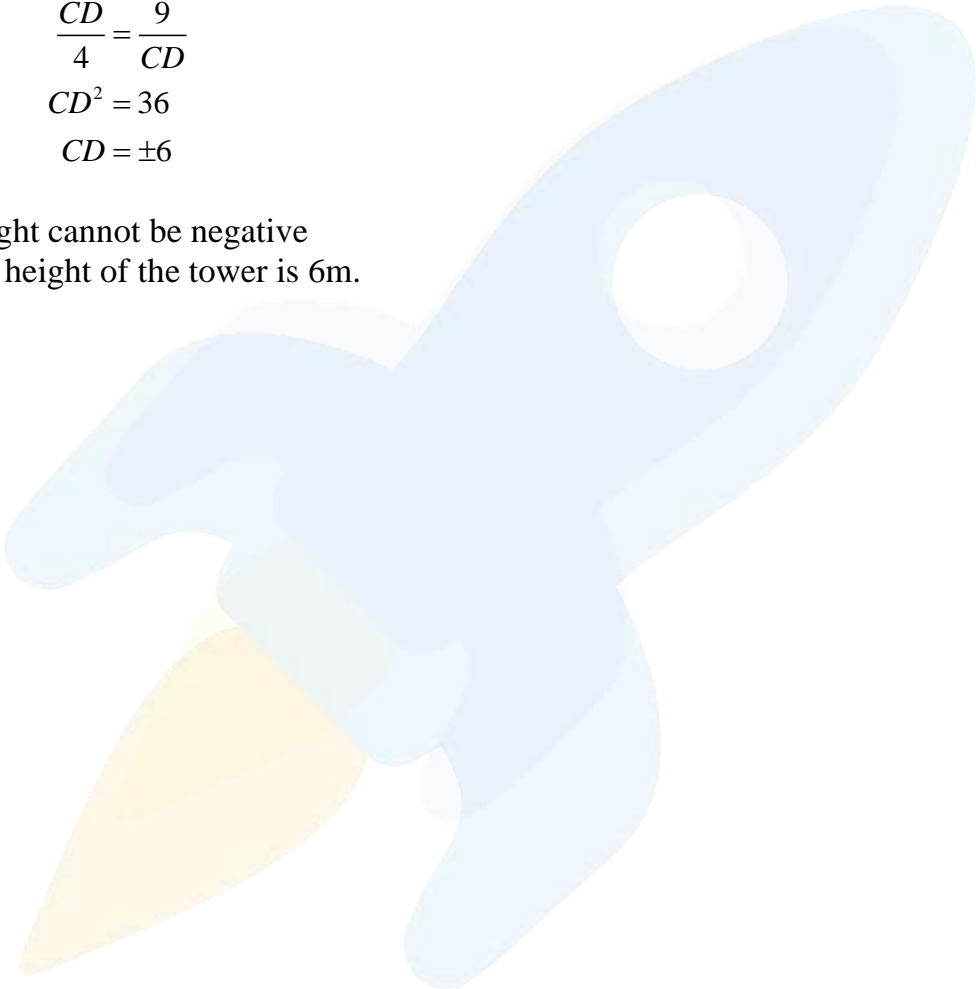
From equation (1) and (2)

$$\frac{CD}{4} = \frac{9}{CD}$$

$$CD^2 = 36$$

$$CD = \pm 6$$

Since, Height cannot be negative
Therefore, height of the tower is 6m.



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