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NCERT Solutions Class 12 Maths Chapter 12 Linear Programming

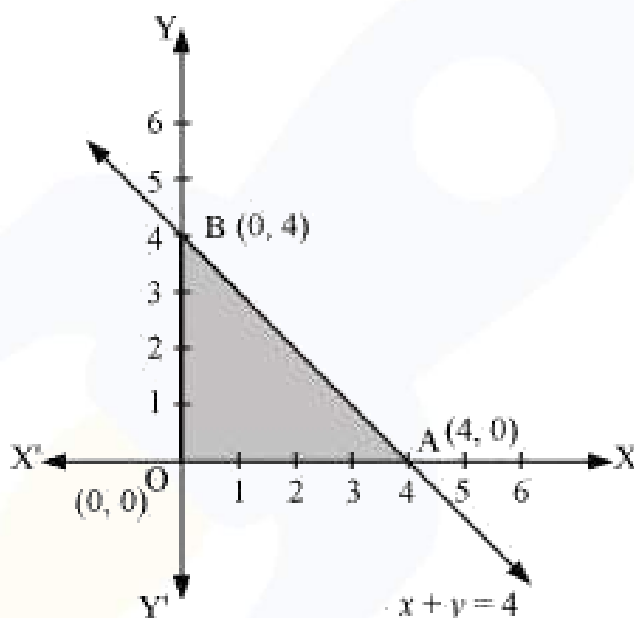
Question 1:

Maximize $Z = 3x + 4y$

Subject to the constraints: $x + y \leq 4, x \geq 0, y \geq 0$

Solution:

The feasible region determined by the constraints, $x + y \leq 4, x \geq 0$ and $y \geq 0$ is given by



Since, the corner points of the feasible region are $O(0,0)$, $A(4,0)$ and $B(0,4)$. The value of Z at these points are as follows:

Corner point	$Z = 3x + 4y$	
$O(0,0)$	0	
$A(4,0)$	12	
$B(0,4)$	16	→ Maximum

Question 2:

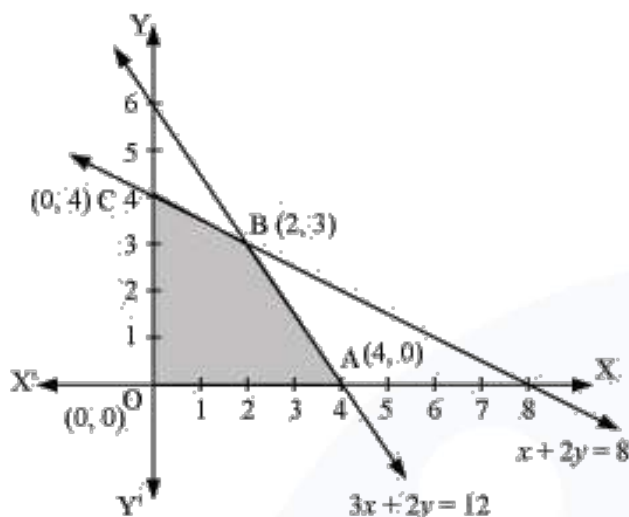
Minimize $Z = -3x + 4y$

Thus, the maximum value of Z is 16 at the point $B(0,4)$.

Subject to $x + 2y \leq 8$, $3x + 2y \leq 12$, $x \geq 0$, $y \geq 0$

Solution:

The feasible region determined by the system of constraints, $x + 2y \leq 8$, $3x + 2y \leq 12$, $x \geq 0$ and $y \geq 0$, is given by



Since, the corner points of the feasible region are $O(0,0)$, $A(4,0)$, $B(2,3)$ and $C(0,4)$. The value of Z at these corner points are as follows:

Corner point	$Z = -3x + 4y$	
$O(0,0)$	0	
$A(4,0)$	-12	→ Minimum
$B(2,3)$	6	
$C(0,4)$	16	

Thus, the minimum value of Z is -12 at the point $A(4,0)$.

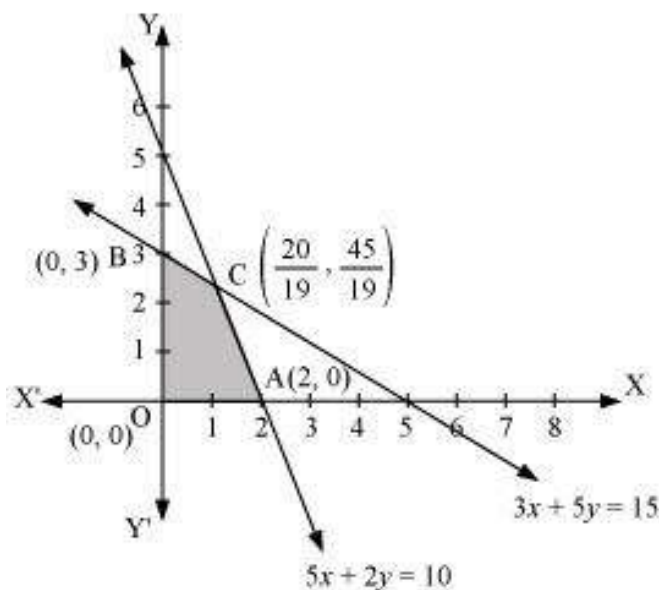
Question 3:

Maximize $Z = 5x + 3y$

Subject to $3x + 5y \leq 15$, $5x + 2y \leq 10$, $x \geq 0$, $y \geq 0$

Solution:

The feasible region determined by the system of constraints $3x + 5y \leq 15$, $5x + 2y \leq 10$, $x \geq 0$ and $y \geq 0$, is given by



Since, the corner points of the feasible region are $O(0,0)$, $A(2,0)$, $B(0,3)$ and $C\left(\frac{20}{19}, \frac{45}{19}\right)$. The value of Z at these corner points are as follows:

Corner point	$Z = 5x + 3y$	
$O(0,0)$	0	
$A(2,0)$	10	
$B(0,3)$	9	
$C\left(\frac{20}{19}, \frac{45}{19}\right)$	$\frac{235}{19}$	→ Maximum

Thus, the maximum value of Z is $\left(\frac{235}{19}\right)$ at the point $C\left(\frac{20}{19}, \frac{45}{19}\right)$.

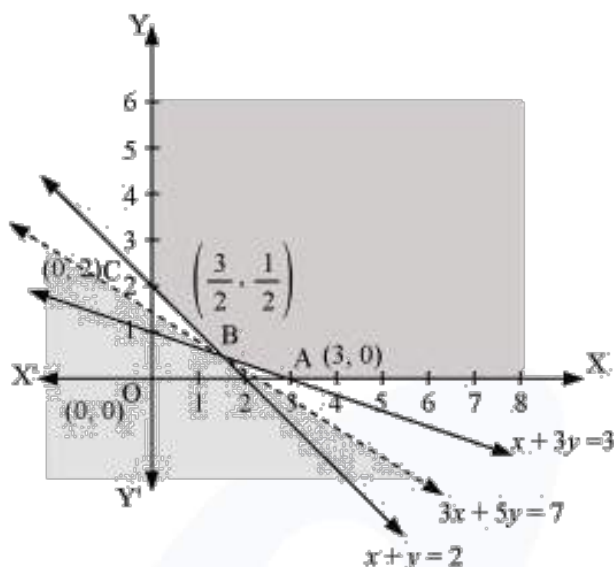
Question 4:

Minimize $Z = 3x + 5y$

Subject to $x + 3y \geq 3$, $x + y \geq 2$, $x, y \geq 0$

Solution:

The feasible region determined by the system of constraints, $x + 3y \geq 3$, $x + y \geq 2$ and $x, y \geq 0$, is given by



Since, the feasible region is unbounded, the corner points of the feasible region are $A(3, 0)$, $B\left(\frac{3}{2}, \frac{1}{2}\right)$ and $C(0, 2)$. The values of Z at these corner points are as follows:

Corner point	$Z = 3x + 5y$	
$A(3, 0)$	9	
$B\left(\frac{3}{2}, \frac{1}{2}\right)$	7	→ Minimum
$C(0, 2)$	10	

As the feasible region is unbounded, therefore, 7 may or may not be the minimum value of Z . For this, we draw the graph of the inequality, $3x + 5y < 7$, and check whether the resulting half plane has points in common with the feasible region or not.

Since, feasible region has no common point with $3x + 5y < 7$

Thus, the minimum value of Z is 7 at $\left(\frac{3}{2}, \frac{1}{2}\right)$.

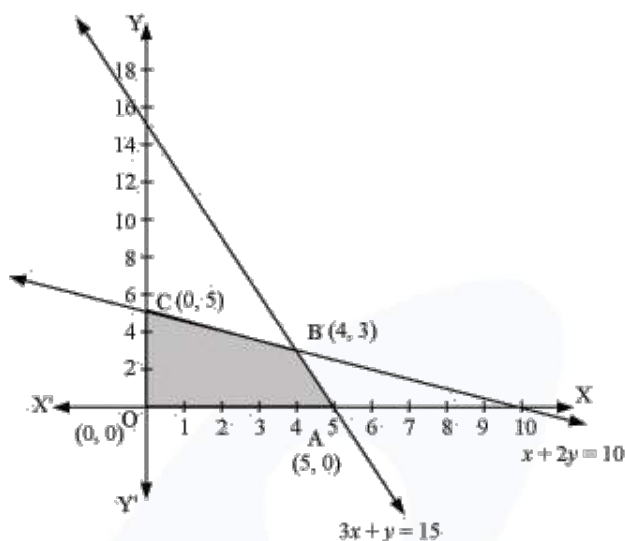
Question 5:

Maximize $Z = 3x + 2y$

Subject to $x + 2y \leq 10$, $3x + y \leq 15$, $x, y \geq 0$

Solution:

The feasible region determined by the constraints, $x + 2y \leq 10$, $3x + y \leq 15$ and $x, y \geq 0$, is given by



Since the corner points of the feasible region are $A(5,0)$, $B(4,3)$ and $C(0,5)$.
 The values of Z at these corner points are as follows:

Corner point	$Z = 3x + 2y$	
$A(5,0)$	15	
$B(4,3)$	18	→ Maximum
$C(0,5)$	10	

Thus, the maximum value of Z is 18 at the point $B(4,3)$.

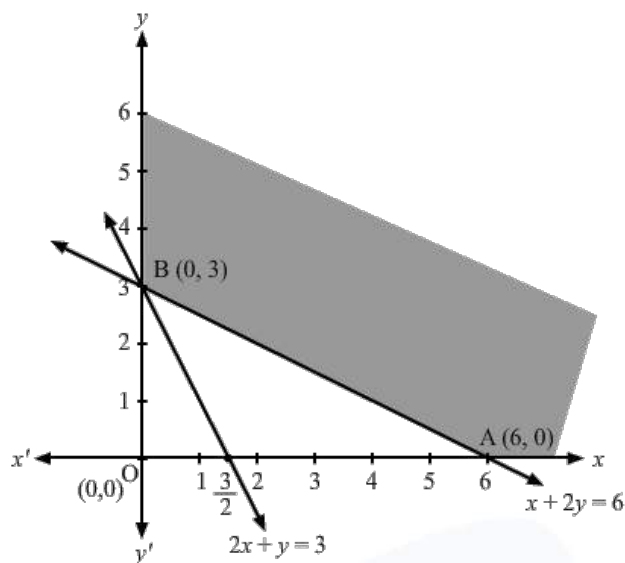
Question 6:

Minimize $Z = x + 2y$

Subject to $2x + y \geq 3$, $x + 2y \geq 6$, $x, y \geq 0$

Solution:

The feasible region determined by the constraints, $2x + y \geq 3$, $x + 2y \geq 6$ and $x, y \geq 0$, is given by



Since the corner points of the feasible region are $A(6,0)$ and $B(0,3)$.
 The values of Z at these corner points are as follows:

Corner point	$Z = x + 2y$
$A(6,0)$	6
$B(0,3)$	6

Since the values of Z at points A and B is same. If we take any other point such as $(2,2)$ on line $x + 2y = 6$, then $Z = 6$.

Thus, the minimum value of Z occurs for more than 2 points.

Thus, the value of Z is minimum at every point on the line, $x + 2y = 6$.

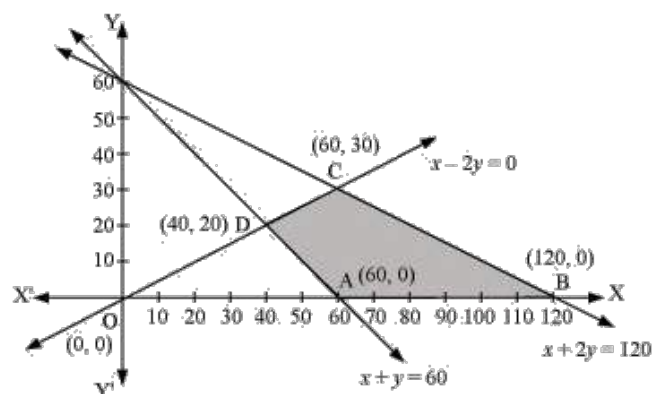
Question 7:

Minimize and Maximize $Z = 5x + 10y$

subject to $x + 2y \leq 120$, $x + y \geq 60$, $x - 2y \geq 0$, $x, y \geq 0$

Solution:

The feasible region determined by the constraints, $x + 2y \leq 120$, $x + y \geq 60$, $x - 2y \geq 0$ and $x, y \geq 0$ is given by



Since the corner points of the feasible region are $A(60,0)$, $B(120,0)$, $C(60,30)$ and $D(40,20)$. The values of Z at these corner points are as follows:

Corner point	$Z = 5x + 10y$	
$A(60,0)$	300	→ Minimum
$B(120,0)$	600	→ Maximum
$C(60,30)$	600	→ Maximum
$D(40,20)$	400	

The minimum value of Z is 300 at $A(60,0)$ and the maximum value of Z is 600 at all the points on the line segment joining $B(120,0)$ and $C(60,30)$.

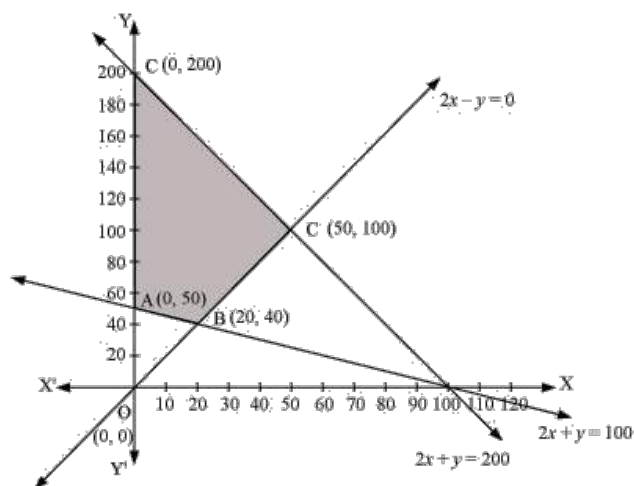
Question 8:

Minimize and Maximize $Z = x + 2y$

Subject to $x + 2y \geq 100$, $2x - y \leq 0$, $2x + y \leq 200$, $x, y \geq 0$

Solution:

The feasible region determined by the constraints, $x + 2y \geq 100$, $2x - y \leq 0$, $2x + y \leq 200$ and $x, y \geq 0$ is given by



The corner points of the feasible region are $A(0,50)$, $B(20,40)$, $C(50,100)$ and $D(0,200)$.
 The values of Z at these corner points are as follows:

Corner point	$Z = x + 2y$	
$A(0,50)$	100	→ Minimum
$B(20,40)$	100	→ Minimum
$C(50,100)$	250	
$D(0,200)$	400	→ Maximum

The maximum value of Z is 400 at $D(0,200)$ and the minimum value of Z is 100 at all the points on the line segment joining $A(0,50)$ and $B(20,40)$.

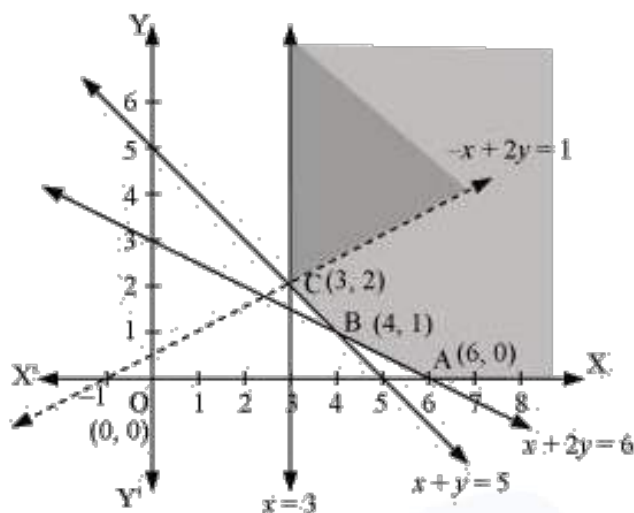
Question 9:

Maximize $Z = -x + 2y$

subject to the constraints: $x \geq 3$, $x + y \geq 5$, $x + 2y \geq 6$, $y \geq 0$

Solution:

The feasible region determined by the constraints, $x \geq 3$, $x + y \geq 5$, $x + 2y \geq 6$ and $y \geq 0$, is given by



Since, the feasible region is unbounded, the values of Z at corner points $A(6,0)$, $B(4,1)$ and $C(3,2)$ are as follows:

Corner point	$Z = -x + 2y$
$A(6,0)$	$Z = -6$
$B(4,1)$	$Z = -2$
$C(3,2)$	$Z = 1$

As the feasible region is unbounded, therefore, $Z = 1$ may or may not be the maximum value. For this, we graph the inequality, $-x + 2y > 1$, and check whether the resulting half plane has points in common with the feasible region or not.

The resulting feasible region has points in common with the feasible region.

Thus, $Z = 1$ is not the maximum value.

Therefore, Z has no maximum value.

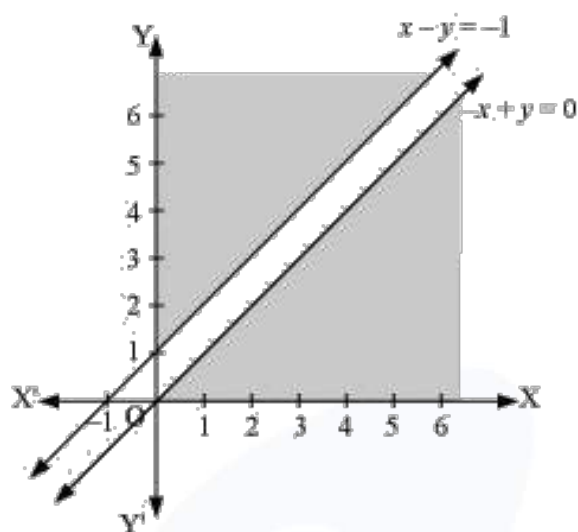
Question 10:

Maximize $Z = x + y$

Subject to $x - y \leq -1$, $-x + y \leq 0$, $x, y \geq 0$

Solution:

The feasible region determined by the constraints, $x - y \leq -1$, $-x + y \leq 0$ and $x, y \geq 0$, is given by



There is no feasible region and thus, Z has no maximum value.

EXERCISE 12.2

Question 1:

Reshma wishes to mix two types of food P and Q in such a way that the vitamin contents of the mixture contain at least 8 units of vitamin A and 11 units of vitamin B. Food P costs ₹ 60/kg and Food Q costs ₹ 80/kg. Food P contains 3 units/kg of vitamin A and 5 units/kg of vitamin B while food Q contains 4 units/kg of vitamin A and 2 units/kg of vitamin B. Determine the minimum cost of the mixture.

Solution:

Let the mixture contain x kg of food P and y kg of food Q.

Therefore, $x \geq 0$ and $y \geq 0$.

The given information can be shown in a table as follows:

	Vitamin A (units/kg)	Vitamin B (units/kg)	Cost (₹/kg)
Food P	3	5	60
Food Q	4	2	80
Requirement (units/kg)	8	11	

The mixture must contain at least 8 units of Vitamin A and 11 units of Vitamin B. Thus, the constraints are

$$3x + 4y \geq 8$$

$$5x + 2y \geq 11$$

Total cost, Z , of purchasing food is

$$Z = 60x + 80y$$

The mathematical formulation of the given problem is

Minimize

$$Z = 60x + 80y \quad \dots(1)$$

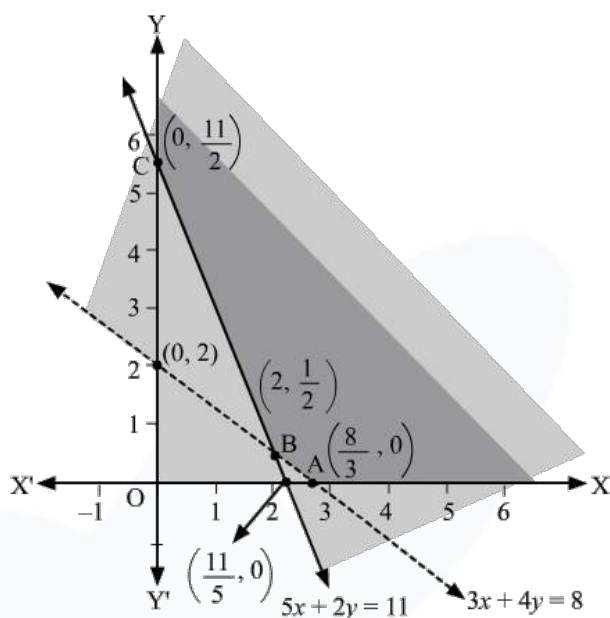
Subject to the constraints,

$$3x + 4y \geq 8 \quad \dots(2)$$

$$5x + 2y \geq 11 \quad \dots(3)$$

$$x, y \geq 0 \quad \dots(4)$$

The feasible region determined by the system of constraints is given by



Since, the feasible region is unbounded.

The corner points of the feasible region are $A\left(\frac{8}{3}, 0\right)$, $B\left(2, \frac{1}{2}\right)$ and $C\left(0, \frac{11}{2}\right)$.
 The values of Z at these corner points are as follows:

Corner point	$Z = 60x + 80y$	
$A\left(\frac{8}{3}, 0\right)$	160	} \rightarrow Minimum
$B\left(2, \frac{1}{2}\right)$	160	
$C\left(0, \frac{11}{2}\right)$	440	

As the feasible region is unbounded, therefore, 160 may or may not be the minimum value of Z .

For this, we graph the inequality, $60x + 80y < 160$ or $3x + 4y < 8$ and check whether the resulting half plane has points in common with the feasible region or not.

Since, the feasible region has no common point with $3x + 4y < 8$

Thus, the minimum cost of the mixture will be ₹ 160 at the line segment joining the points

$$\left(\frac{8}{3}, 0\right) \text{ and } \left(2, \frac{1}{2}\right).$$

Question 2:

One kind of cake requires 200g flour and 25g of fat, and another kind of cake requires 100g of flour and 50g of fat. Find the maximum number of cakes which can be made from 5 kg of flour and 1 kg of fat assuming that there is no shortage of the other ingredients used in making the cakes.

Solution:

Let there be x cakes of first kind and y cakes of second kind.

Therefore, $x \geq 0$ and $y \geq 0$.

The given information can be shown in a table as follows:

	Flour (g)	Fat (g)
Cakes of first kind, x	200	25
Cakes of second kind, y	100	50
Availability	5000	1000

Hence,

$$200x + 100y \leq 5000$$

$$\Rightarrow 2x + y \leq 50$$

And

$$25x + 50y \leq 1000$$

$$\Rightarrow x + 2y \leq 40$$

Total number of cakes, Z , that can be made are,

$$Z = x + y$$

The mathematical formulation of the given problem is

Maximize,

$$Z = x + y \quad \dots(1)$$

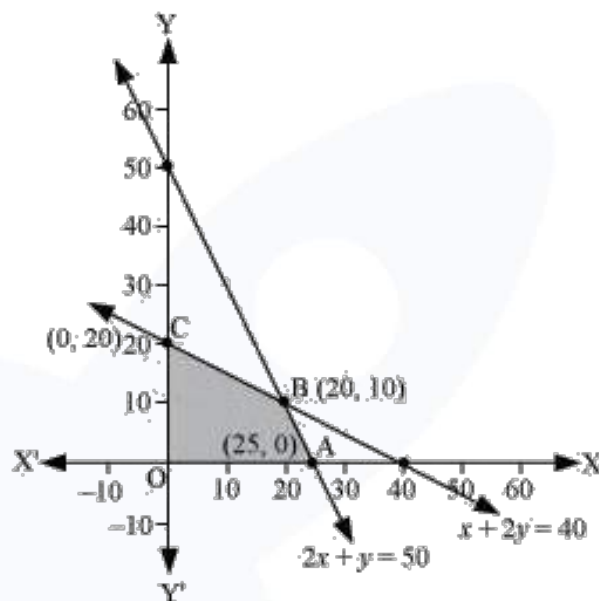
Subject to the constraints,

$$2x + y \leq 50 \quad \dots(2)$$

$$x + 2y \leq 40 \quad \dots(3)$$

$$x, y \geq 0 \quad \dots(4)$$

The feasible region determined by the system of constraints is given by



The corner points are $A(25, 0)$, $B(20, 10)$, $O(0, 0)$ and $C(0, 20)$.

The value of Z at these corner points are as follows:

Corner point	$Z = x + y$	
$A(25, 0)$	25	
$B(20, 10)$	30	→ Maximum
$O(0, 0)$	0	
$C(0, 20)$	20	

Thus, the maximum number of cakes that can be made are 30 (20 of one kind and 10 of the other kind).

Question 3:

A factory makes tennis rackets and cricket bats. A tennis racket takes 1.5 hours of machine time and 3 hours of craftsman's time in its making while a cricket bat takes 3 hour of machine time and 1 hour of craftsman's time. In a day, the factory has the availability of not more than 42 hours of machine time and 24 hours of craftsman's time.

- What number of rackets and bats must be made if the factory is to work at full capacity?
- If the profit on a racket and on a bat is ₹ 20 and ₹ 10 respectively, find the maximum profit of the factory when it works at full capacity.

Solution:

- Let the number of rackets and the number of bats to be made are x and y , respectively. The machine time is not available for more than 42 hours. Therefore,

$$1.5x + 3y \leq 42 \quad \dots(1)$$

The craftsman's time is not available for more than 24 hours.

$$3x + y \leq 24 \quad \dots(2)$$

The factory is to work at full capacity. Therefore,

$$1.5x + 3y = 42$$

$$3x + y = 24$$

On solving these equations, we obtain

$$x = 4 \text{ and } y = 12$$

Thus, 4 rackets and 12 bats must be made.

- The given information can be shown in a table as follows:

	Tennis Racket	Cricket Bat	Availability
Machine Time (h)	1.5	3	42
Craftsman's Time (h)	3	1	24

Hence,

$$1.5x + 3y \leq 42$$

$$3x + y \leq 24$$

$$x, y \geq 0$$

The profit on a racket is ₹ 20 and on bat is ₹ 10

Maximize

$$Z = 20x + 10y \quad \dots(1)$$

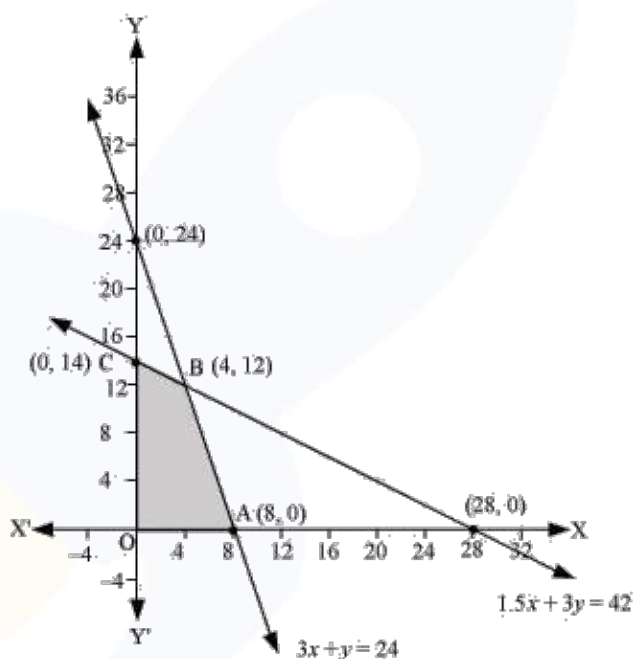
Subject to the constraints,

$$1.5x + 3y \leq 42 \quad \dots(2)$$

$$3x + y \leq 24 \quad \dots(3)$$

$$x, y \geq 0 \quad \dots(4)$$

The feasible region determined by the system of constraints is given by



The corner points are $A(8,0)$, $B(4,12)$, $C(0,14)$ and $O(0,0)$.

The values of Z at these corner points are as follows:

Corner point	$Z = 20x + 10y$	
$A(8,0)$	160	
$B(4,12)$	200	→ Maximum
$C(0,14)$	140	

$O(0,0)$	0	
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Thus, the maximum profit of the factory when it works to its full capacity is ₹ 200.

Question 4:

A manufacturer produces nuts and bolts. It takes 1 hour of work on machine A and 3 hours on machine B to produce a package of nuts. It takes 3 hours on machine A and 1 hour on machine B to produce a package of bolts. He earns a profit, of ₹ 17.50 per package on nuts and ₹ 7.00 per package on bolts. How many packages of each should be produced each day so as to maximize his profit, if he operates his machines for at the most 12 hours a day?

Solution:

Let the manufacturer produce x packages of nuts and y packages of bolts.

Therefore, $x \geq 0$ and $y \geq 0$

The given information can be shown in a table as follows:

	Nuts	Bolts	Availability
Machine A (h)	1	3	12
Machine B (h)	3	1	12

The profit on a package of nuts is ₹ 17.50 and on a package of bolts is ₹ 7.

Therefore, the constraints are

$$x + 3y \leq 12$$

$$3x + y \leq 12$$

Total profit,

$$Z = 17.5x + 7y$$

The mathematical formulation of the given problem is

Maximize

$$Z = 17.5x + 7y \quad \dots(1)$$

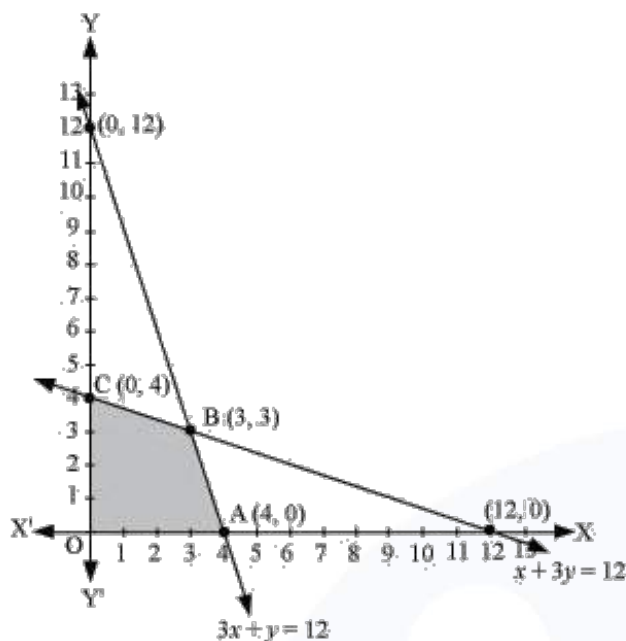
Subject to the constraints,

$$x + 3y \leq 12 \quad \dots(2)$$

$$3x + y \leq 12 \quad \dots(3)$$

$$x, y \geq 0 \quad \dots(4)$$

The feasible region determined by the system of constraints is given by



The corner points are $O(0,0)$, $A(4,0)$, $B(3,3)$ and $C(0,4)$.

The values of Z at these corner points are as follows:

Corner point	$Z = 17.5x + 7y$	
$O(0,0)$	0	
$A(4,0)$	70	
$B(3,3)$	73.5	→ Maximum
$C(0,4)$	28	

The maximum value of Z is ₹ 73.50 at $B(3,3)$.

Question 5:

A factory manufactures two types of screws, A and B. Each type of screw requires the use of two machines, an automatic and a hand operated. It takes 4 minutes on the automatic and 6 minutes on hand operated machines to manufacture a package of screws A, while it takes 6

minutes on automatic and 3 minutes on the hand operated machines to manufacture a package of screws B. Each machine is available for at the most 4 hours on any day. The manufacturer can sell a package of screws A at a profit of ₹ 7 and screws B at a profit of ₹ 10. Assuming that he can sell all the screws he manufactures, how many packages of each type should the factory owner produce in a day in order to maximize his profit? Determine the maximum profit.

Solution:

Let the factory manufacture x screws of type A and y screws of type B on each day.

Therefore, $x \geq 0$ and $y \geq 0$

The given information can be shown in a table as follows:

	Screw A	Screw B	Availability
Automatic Machine (min.)	4	6	$4 \times 60 = 240$
Hand Operated Machine (min.)	6	3	$4 \times 60 = 240$

The profit on a package of screws A is ₹ 7 and on the package of screws B is ₹ 10.

Therefore, the constraints are

$$4x + 6y \leq 240$$

$$6x + 3y \leq 240$$

Total profit,

$$Z = 7x + 10y$$

The mathematical formulation of the given problem is

Maximize

$$Z = 7x + 10y \quad \dots(1)$$

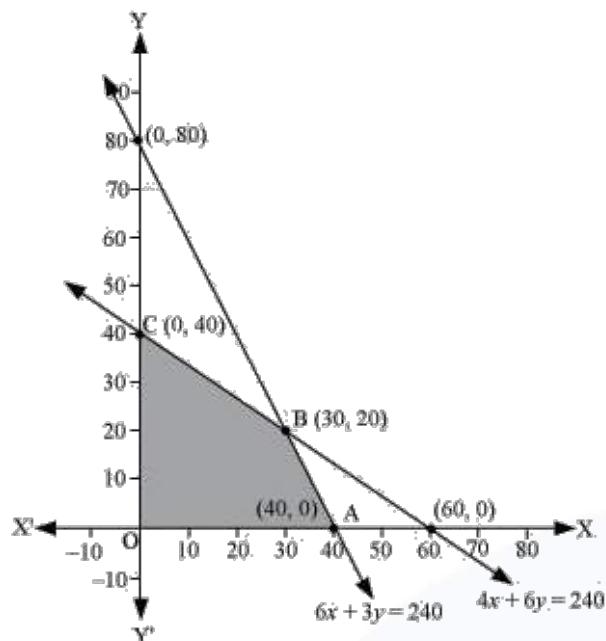
Subject to the constraints,

$$4x + 6y \leq 240 \quad \dots(2)$$

$$6x + 3y \leq 240 \quad \dots(3)$$

$$x, y \geq 0 \quad \dots(4)$$

The feasible region determined by the system of constraints is given by



The corner points are $A(40, 0)$, $B(30, 20)$ and $C(0, 40)$.
 The values of Z at these corner points are as follows:

Corner point	$Z = 7x + 10y$	
$A(40, 0)$	280	
$B(30, 20)$	410	→ Maximum
$C(0, 40)$	400	

The maximum value of Z is 410 at $B(30, 20)$.

Question 6:

A cottage industry manufactures pedestal lamps and wooden shades, each requiring the use of a grinding /cutting machine and a sprayer. It takes 2 hours on grinding /cutting machine and 3 hours on the sprayer to manufacture a pedestal lamp. It takes 1 hour on the grinding /cutting machine and 2 hours on the sprayer to manufacture a shade. On any day, the sprayer is available for at the most 20 hours and the grinding/cutting machine for at the most 12 hours. The profit from the sale of a lamp is ₹ 5 and that from a shade is ₹ 3. Assuming that the manufacturer can sell all the lamps and shades that he produces, how should he schedule his daily production in order to maximize his profit?

Solution:

Let the cottage industry manufacture x pedestal lamps and y wooden shades.

Therefore, $x \geq 0$ and $y \geq 0$

The given information can be shown in a table as follows:

	Lamps	Shades	Availability
Grinding/Cutting Machine (h)	2	1	12
Sprayer (h)	3	2	20

The profit on a lamp is ₹ 5 and on the shades is ₹ 3.

Therefore, the constraints are

$$2x + y \leq 12$$

$$3x + 2y \leq 20$$

Total profit,

$$Z = 5x + 3y$$

The mathematical formulation of the given problem is

Maximize

$$Z = 5x + 3y \quad \dots(1)$$

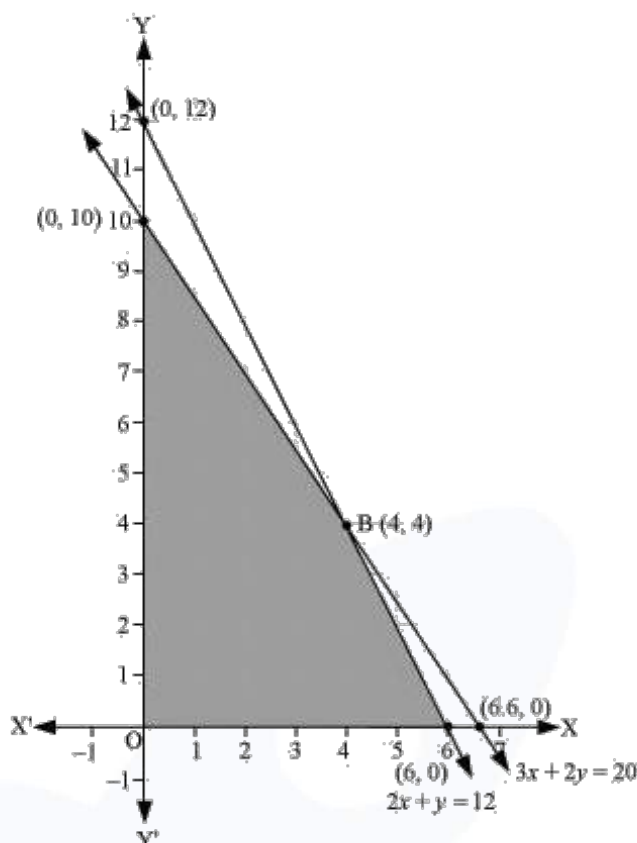
Subject to the constraints,

$$2x + y \leq 12 \quad \dots(2)$$

$$3x + 2y \leq 20 \quad \dots(3)$$

$$x, y \geq 0 \quad \dots(4)$$

The feasible region determined by the system of constraints is given by



The corner points are $A(6, 0)$, $B(4, 4)$ and $C(0, 10)$.
 The values of Z at these corner points are as follows:

Corner point	$Z = 5x + 3y$	
$A(6, 0)$	30	
$B(4, 4)$	32	→ Maximum
$C(0, 10)$	30	

The maximum value of Z is 32 at $B(4, 4)$.

Therefore, the manufacturer should produce 4 pedestal lamps and 4 wooden shades to maximize his profits.

Question 7:

A company manufactures two types of novelty Souvenirs made of plywood. Souvenirs of type A require 5 minutes each for cutting and 10 minutes each for assembling. Souvenirs of type B require 8 minutes each for cutting and 8 minutes each for assembling. There are 3 hours 20 minutes available for cutting and 4 hours of assembling. The profit is ₹ 5 each for type A and

₹ 6 each for type B Souvenirs. How many Souvenirs of each type should the company manufacture in order to maximize the profit?

Solution:

Let the company manufacture x Souvenirs of type A and y Souvenirs of type B.

Therefore, $x \geq 0$ and $y \geq 0$.

The given information can be shown in a table as follows:

	Type A	Type B	Availability
Cutting (min.)	5	8	$3 \times 60 + 20 = 200$
Assembling (min.)	10	8	$4 \times 60 = 240$

The profit on type A Souvenirs is ₹ 5 and type B Souvenirs is ₹ 6.

Therefore, the constraints are

$$5x + 8y \leq 200$$

And

$$10x + 8y \leq 240$$

$$\Rightarrow 5x + 4y \leq 120$$

Total profit,

$$Z = 5x + 6y$$

The mathematical formulation of the given problem is

Maximize

$$Z = 5x + 6y \quad \dots(1)$$

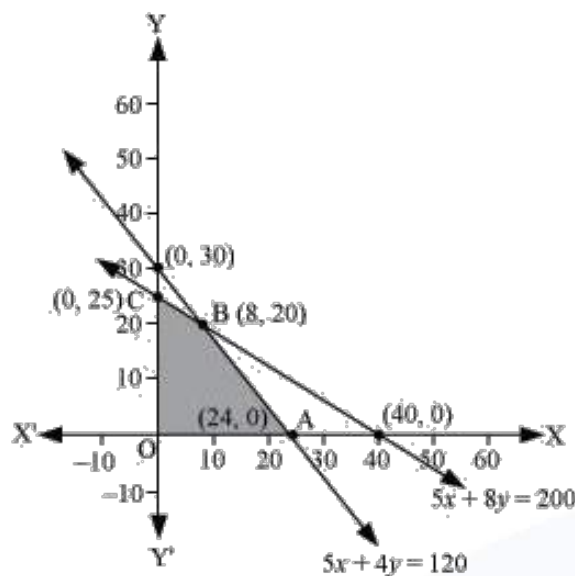
Subject to the constraints,

$$5x + 8y \leq 200 \quad \dots(2)$$

$$5x + 4y \leq 120 \quad \dots(3)$$

$$x, y \geq 0 \quad \dots(4)$$

The feasible region determined by the system of constraints is given by



The corner points are $A(24, 0)$, $B(8, 20)$ and $C(0, 25)$.

The values of Z at these corner points are as follows:

Corner point	$Z = 5x + 6y$	
$A(24, 0)$	120	
$B(8, 20)$	160	→ Maximum
$C(0, 25)$	150	

The maximum value of Z is 160 at $B(8, 20)$.

Hence, 8 Souvenirs of type A and 20 Souvenirs of type B should be produced each day to get the maximum profit of ₹ 160.

Question 8:

A merchant plans to sell two types of personal computers – a desktop model and a portable model that will cost ₹ 25000 and ₹ 40000 respectively. He estimates that the total monthly demand of computers will not exceed 250 units. Determine the number of units of each type of computers which the merchant should stock to get maximum profit if he does not want to invest more than ₹ 70 lakhs and if his profit on the desktop model is ₹ 4500 and on portable model is ₹ 5000.

Solution:

Let the merchant stock x desktop models and y portable models.

Therefore, $x \geq 0$ and $y \geq 0$

The cost of a desktop model is ₹ 25000 and of a portable model is ₹ 4000. However, the merchant can invest a maximum of ₹ 70 lakhs.

Therefore,

$$25000x + 40000y \leq 7000000$$

$$\Rightarrow 5x + 8y \leq 1400$$

The monthly demand of computers will not exceed 250 units.

Therefore,

$$x + y \leq 250$$

The profit on a desktop model is ₹ 4500 and the profit on a portable model is ₹ 5000.

Total profit,

$$Z = 4500x + 5000y$$

Thus, the mathematical formulation of the given problem is

Maximize

$$Z = 4500x + 5000y \quad \dots(1)$$

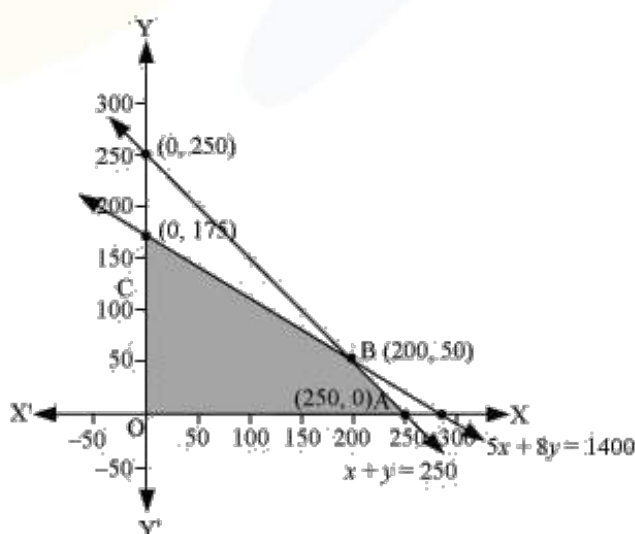
Subject to the constraints,

$$5x + 8y \leq 1400 \quad \dots(2)$$

$$x + y \leq 250 \quad \dots(3)$$

$$x, y \geq 0 \quad \dots(4)$$

The feasible region determined by the system of constraints is given by



The corner points are $A(250, 0)$, $B(200, 50)$ and $C(0, 175)$.

The values of Z at these corner points are as follows:

Corner point	$Z = 4500x + 5000y$	
A(250,0)	1125000	
B(200,50)	1150000	→ Maximum
C(0,175)	875000	

The maximum value of Z is 1150000 at $B(200,50)$.

Therefore, the merchant should stock 200 desktop models and 50 portable models to get the maximum profit of ₹ 1150000.

Question 9:

A diet is to contain at least 80 units of vitamin A and 100 units of minerals. Two foods F_1 and F_2 are available. Food F_1 costs ₹ 4 per unit food and F_2 costs ₹ 6 per unit. One unit of food F_1 contains 3 units of vitamin A and 4 units of minerals. One unit of food F_2 contains 6 units of vitamin A and 3 units of minerals. Formulate this as a linear programming problem. Find the minimum cost for diet that consists of mixture of these two foods and also meets the minimal nutritional requirements.

Solution:

Let the diet contain x units of food F_1 and y units of food F_2 .

Therefore, $x \geq 0$ and $y \geq 0$

The given information can be shown in a table as follows:

	Vitamin A (units)	Mineral (units)	Cost per unit (₹)
Food F_1 (x)	3	4	4
Food F_2 (y)	6	3	6
Requirement	80	100	

The cost of food F_1 is ₹ 4/unit and of food F_2 is ₹ 6/unit.

Therefore, the constraints are

$$3x + 6y \geq 80$$

$$4x + 3y \geq 100$$

$$x, y \geq 0$$

Total cost of the diet,

$$Z = 4x + 6y$$

The mathematical formulation of the given problem is

Minimize

$$Z = 4x + 6y \quad \dots(1)$$

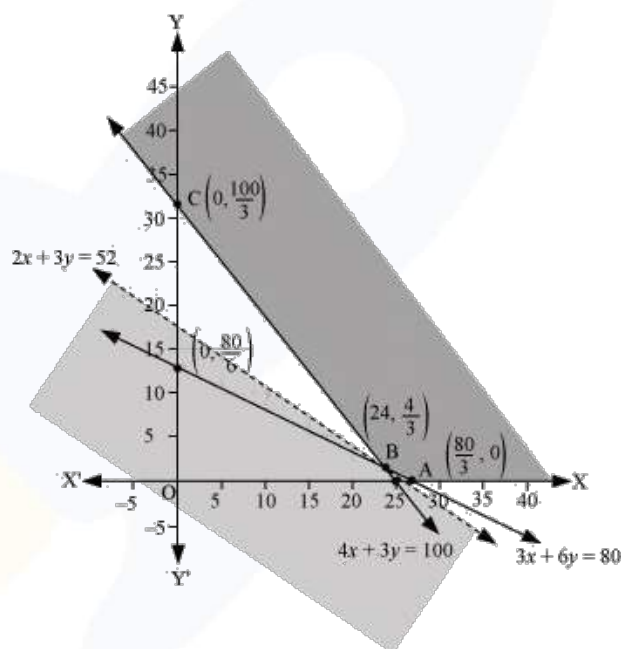
Subject to the constraints,

$$3x + 6y \geq 80 \quad \dots(2)$$

$$4x + 3y \geq 100 \quad \dots(3)$$

$$x, y \geq 0 \quad \dots(4)$$

The feasible region determined by the constraints is given by



Since, the feasible region is unbounded.

The corner points of the feasible region are $A\left(\frac{80}{3}, 0\right)$, $B\left(24, \frac{4}{3}\right)$ and $C\left(0, \frac{100}{3}\right)$.
 The values of Z at these corner points are as follows:

Corner point	$Z = 4x + 6y$	
$A\left(\frac{80}{3}, 0\right)$	$\frac{320}{3} = 106.67$	
$B\left(24, \frac{4}{3}\right)$	104	→ Minimum
$C\left(0, \frac{100}{3}\right)$	200	

As the feasible region is unbounded, therefore, 104 may or may not be the minimum value of Z .

For this, we draw a graph of the inequality, $4x + 6y < 104$ or $2x + 3y < 52$, and check whether the resulting half plane has points in common with the feasible region or not.

Since, the feasible region has no common point with $2x + 3y < 52$.

Therefore, the minimum cost of the mixture will be ₹ 104.

Question 10:

There are two types of fertilizers F_1 and F_2 . F_1 consists of 10% nitrogen and 6% phosphoric acid and F_2 consists of 5% nitrogen and 10% phosphoric acid. After testing the soil conditions, a farmer finds that she needs at least 14 kg of nitrogen and 14 kg of phosphoric acid for her crop. If F_1 cost ₹ 6/kg and F_2 costs ₹5/kg, determine how much of each type of fertilizer should be used so that nutrient requirements are met at a minimum cost. What is the minimum cost?

Solution:

Let the farmer buy x kg of fertilizer F_1 and y kg of fertilizer F_2 .

Therefore, $x \geq 0$ and $y \geq 0$

The given information can be shown in a table as follows:

	Nitrogen (%)	Phosphoric Acid (%)	Cost (₹/kg)
$F_1 (x)$	10	6	6
$F_2 (y)$	5	10	5
Requirement (kg)	14	14	

F_1 consists of 10% nitrogen and F_2 consists of 5% nitrogen. However, the farmer requires at least 14 kg of nitrogen.

Therefore,

$$10\% \text{ of } x + 5\% \text{ of } y \geq 14$$

$$\frac{x}{10} + \frac{y}{20} \geq 14$$

$$2x + y \geq 280$$

F_1 consists of 6% phosphoric acid and F_2 consists of 10% phosphoric acid.

However, the farmer requires at least 14 kg of phosphoric acid.

Therefore,

$$6\% \text{ of } x + 10\% \text{ of } y \geq 14$$

$$\frac{6x}{100} + \frac{10y}{100} \geq 14$$

$$3x + 5y \geq 700$$

Total cost of fertilizers,

$$Z = 6x + 5y$$

The mathematical formulation of the given problem is

Minimize

$$Z = 6x + 5y \quad \dots(1)$$

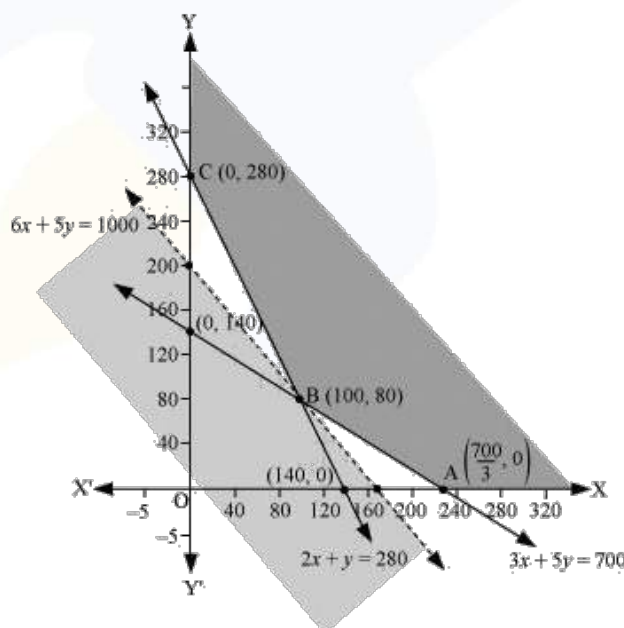
Subject to the constraints,

$$2x + y \geq 280 \quad \dots(2)$$

$$3x + 5y \geq 700 \quad \dots(3)$$

$$x, y \geq 0 \quad \dots(4)$$

The feasible region determined by the system of constraints is given by



Since, the feasible region is unbounded.

The corner points are $A\left(\frac{700}{3}, 0\right)$, $B(100, 80)$ and $C(0, 280)$.

The values of Z at these corner points are as follows:

Corner point	$Z = 6x + 5y$	
$A\left(\frac{700}{3}, 0\right)$	1400	
$B(100, 80)$	1000	\rightarrow Minimum
$C(0, 280)$	1400	

As the feasible region is unbounded, therefore, 1000 may or may not be the minimum value of Z .

For this, we draw a graph of the inequality, $6x + 5y < 1000$, and check whether the resulting half plane has points in common with the feasible region or not.

Since, the feasible region has no common point with $6x + 5y < 1000$.

Thus, 100 kg of fertilizer F_1 and 80 kg of fertilizer F_2 should be used to minimize the cost. The minimum cost is ₹ 1000.

Question 11:

The corner points of the feasible region determined by the following system of linear inequalities:

$2x + y \leq 10, x + 3y \leq 15, x, y \geq 0$ are $(0, 0), (5, 0), (3, 4)$ and $(0, 5)$. Let $Z = px + qy$, where $p, q > 0$.

Condition on p and q so that the maximum of Z occurs at both $(3, 4)$ and $(0, 5)$ is

- (A) $p = q$ (B) $p = 2q$ (C) $p = 3q$ (D) $q = 3p$

Solution:

The maximum value of Z is unique.

It is given that the maximum value of Z occurs at two points, $(3, 4)$ and $(0, 5)$.

Therefore, Value of Z at $(3, 4) =$ Value of Z at $(0, 5)$

$$\Rightarrow p(3) + q(4) = p(0) + q(5)$$

$$\Rightarrow 3p + 4q = 5q$$

$$\Rightarrow q = 3p$$

Thus, the correct option is (D).

MISCELLANEOUS EXERCISE

Question 1:

Refer to Example 9 (Diet problem) A dietician has to develop a special diet using two foods P and Q. Each packet (containing 30 g) of food P contains 12 units of calcium, 4 units of iron, 6 units of cholesterol and 6 units of vitamin A. Each packet of the same quantity of food Q contains 3 units of calcium, 20 units of iron, 4 units of cholesterol and 3 units of vitamin A. The diet requires at least 240 units of calcium, at least 460 units of iron and at most 300 units of cholesterol.

How many packets of each food should be used to maximize the amount of vitamin A in the diet? What is the maximum amount of vitamin A in the diet?

Solution:

Let the diet contain x and y packets of foods P and Q respectively.

Thus, $x \geq 0$ and $y \geq 0$

The mathematical formulation of the given problem is as follows.

Maximize

$$Z = 6x + 3y \quad \dots(1)$$

Subject to the constraints,

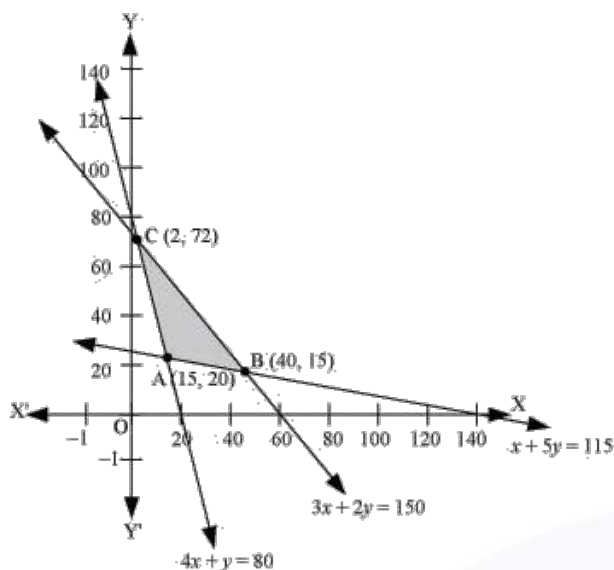
$$4x + y \geq 80 \quad \dots(2)$$

$$x + 5y \geq 115 \quad \dots(3)$$

$$3x + 2y \leq 150 \quad \dots(4)$$

$$x, y \geq 0 \quad \dots(5)$$

The feasible region determined by the system of constraints is given by



The corner points of the feasible region are $A(15, 20)$, $B(40, 15)$ and $C(2, 72)$.

The values of Z at these corner points are as follows:

Corner point	$Z = 6x + 3y$	
$A(15, 20)$	150	
$B(40, 15)$	285	→ Maximum
$C(2, 72)$	228	

Thus, the maximum value of Z is 285 at $B(40, 15)$.

Hence, to maximize the amount of Vitamin A in the diet, 40 packets of Food P and 15 packets of Food Q should be used.

Thus, the maximum amount of Vitamin A in the diet is 285 units.

Question 2:

A farmer mixes two brands P and Q of cattle feed. Brand P, costing ₹ 250 per bag contains 3 units of nutritional element A, 2.5 units of element B and 2 units of element C. Brand Q costing ₹ 200 per bag contains 1.5 units of nutritional elements A, 11.25 units of element B, and 3 units of element C. The minimum requirements of nutrients A, B and C are 18 units, 45 units and 24 units respectively. Determine the number of bags of each brand which should be mixed in order to produce a mixture having a minimum cost per bag? What is the minimum cost of the mixture per bag?

Solution:

Let the farmer mix x bags of brand P and y bags of brand Q.
 The given information can be given in a table as follows:

	Vitamin A (units/kg)	Vitamin B (units/kg)	Cost (₹/kg)
Food P	3	5	60
Food Q	4	2	80
Requirement (units/kg)	8	11	

The given problem can be formulated as follows:

Minimize

$$Z = 250x + 200y \quad \dots(1)$$

Subject to the constraints,

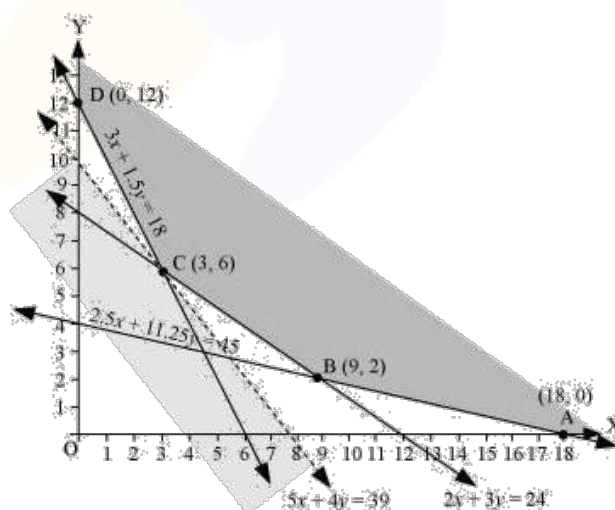
$$3x + 1.5y \geq 18 \quad \dots(2)$$

$$2.5x + 11.25y \geq 45 \quad \dots(3)$$

$$2x + 3y \geq 24 \quad \dots(4)$$

$$x, y \geq 0 \quad \dots(5)$$

The feasible region determined by the system of constraints is given by



The corner points of the feasible region are $A(18,0)$, $B(9,2)$, $C(3,6)$ and $D(0,12)$.
 The values of Z at these corner points are as follows:

Corner point	$Z = 250x + 200y$	
A(18,0)	4500	
B(9,2)	2650	
C(3,6)	1950	→ Minimum
D(0,12)	2400	

As the feasible region is unbounded, therefore, 1950 may or may not be the minimum value of Z .

For this, we draw a graph of the inequality, $250x + 200y < 1950$ or $5x + 4y < 39$, and check whether the resulting half plane has points in common with the feasible region or not.

Since, the feasible region has no common point with $5x + 4y < 39$.

Thus, the minimum value of Z is 1950 at $C(3,6)$.

Therefore, 3 bags of brand P and 6 bags of brand Q should be used in the mixture to minimize the cost to ₹ 1950.

Question 3:

A dietician wishes to mix together two kinds of food X and Y in such a way that the mixture contains at least 10 units of vitamin A, 12 units of vitamin B and 8 units of vitamin C. The vitamin content of one kg food is given below:

Food	Vitamin A	Vitamin B	Vitamin C
X	1	2	3
Y	2	2	1

One kg of food X costs ₹ 16 and one kg of food Y costs ₹ 20. Find the least cost of the mixture which will produce the required diet?

Solution:

Let the mixture contain x kg of food X and y kg of food Y.

The mathematical formulation of the given problem is as follows:

Minimize

$$Z = 16x + 20y \quad \dots(1)$$

Subject to the constraints,

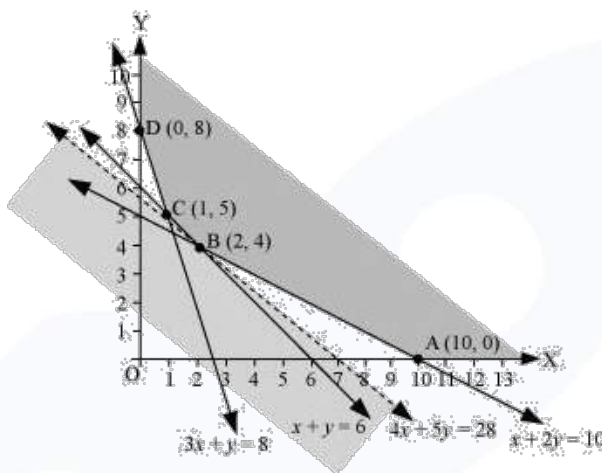
$$x + 2y \geq 10 \quad \dots(2)$$

$$x + y \geq 6 \quad \dots(3)$$

$$3x + y \geq 8 \quad \dots(4)$$

$$x, y \geq 0 \quad \dots(5)$$

The feasible region determined by the system of constraints is given by



The corner points of the feasible region are $A(10, 0)$, $B(2, 4)$, $C(1, 5)$ and $D(0, 8)$.

The values of Z at these corner points are as follows:

Corner point	$Z = 16x + 20y$	
$A(10, 0)$	160	
$B(2, 4)$	112	→ Minimum
$C(1, 5)$	116	
$D(0, 8)$	160	

As the feasible region is unbounded, therefore, 112 may or may not be the minimum value of Z .

For this, we draw a graph of the inequality, $16x + 20y < 112$ or $4x + 5y < 28$, and check whether the resulting half plane has points in common with the feasible region or not.

Since, the feasible region has no common point with $4x + 5y < 28$.

Thus, the minimum value of Z is 112 at $B(2, 4)$.

Therefore, the mixture should contain 2 kg of food X and 4 kg of food Y. The minimum cost of the mixture is ₹ 112.

Question 4:

A manufacturer makes two types of toys A and B. Three machines are needed for this purpose and the time (in minutes) required for each toy on the machines is given below:

Types of Toys	Machines		
	I	II	III
A	12	8	6
B	6	0	9

Each machine is available for a maximum of 6 hours per day. If the profit on each toy of type A is ₹ 7.50 and that on each toy of type B is ₹ 5, show that 15 toys of type A and 30 of type B should be manufactured in a day to get maximum profit.

Solution:

Let x and y toys of type A and type B respectively be manufactured in a day.
 The given problem can be formulated as follows:

Maximize

$$Z = 7.5x + 5y \quad \dots(1)$$

Subject to the constraints,

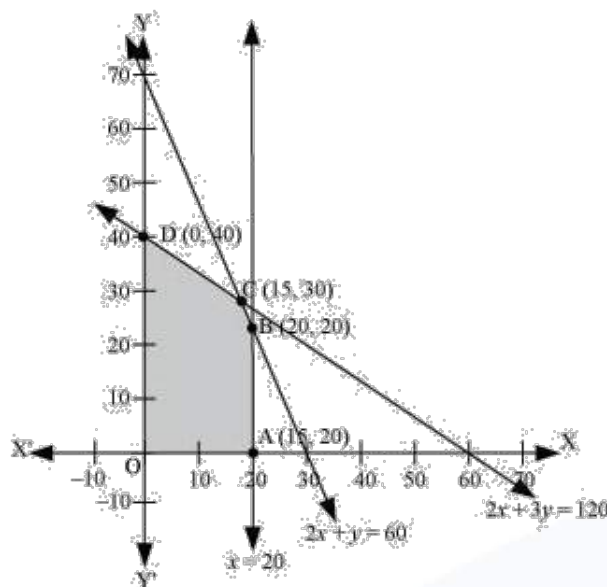
$$2x + y \leq 60 \quad \dots(2)$$

$$x \leq 20 \quad \dots(3)$$

$$2x + 3y \leq 8 \quad \dots(4)$$

$$x, y \geq 0 \quad \dots(5)$$

The feasible region determined by the constraints is given by



The corner points of the feasible region are $A(20,0)$, $B(20,20)$, $C(15,30)$ and $D(0,40)$.
 The values of Z at these corner points are as follows:

Corner point	$Z = 7.5x + 5y$	
$A(20,0)$	150	
$B(20,20)$	250	
$C(15,30)$	262.5	→ Maximum
$D(0,40)$	200	

Thus, the maximum value of Z is 262.5 at $C(15,30)$.

Hence, the manufacturer should manufacture 15 toys of type A and 30 toys of type B to maximize the profit.

Question 5:

An aeroplane can carry a maximum of 200 passengers. A profit of ₹ 1000 is made on each executive class ticket and a profit of ₹ 600 is made on each economy class ticket. The airline reserves at least 20 seats for executive class. However, at least 4 times as many passengers prefer to travel by economy class than by the executive class.

Determine how many tickets of each type must be sold in order to maximize the profit for the airline. What is the maximum profit?

Solution:

Let the airline sell x tickets of executive class and y tickets of economy class.

The mathematical formulation of the given problem is as follows.

Maximize

$$Z = 1000x + 600y \quad \dots(1)$$

Subject to the constraints,

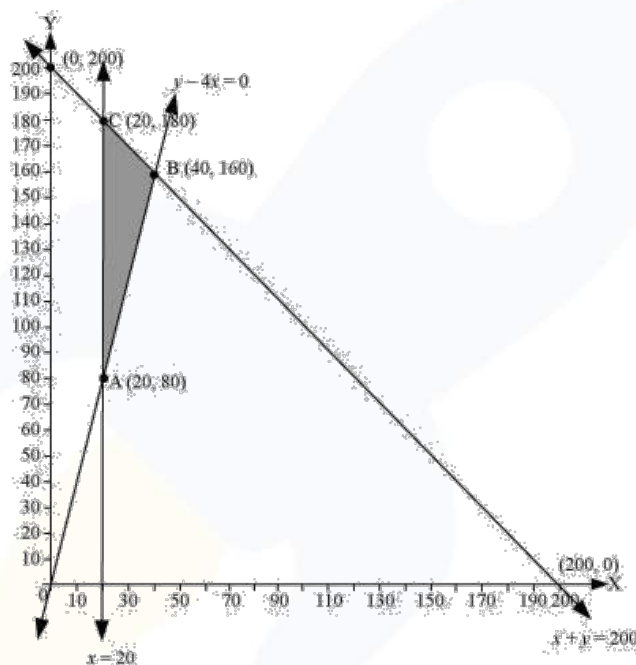
$$x + y \leq 200 \quad \dots(2)$$

$$x \geq 20 \quad \dots(3)$$

$$y - 4x \geq 0 \quad \dots(4)$$

$$x, y \geq 0 \quad \dots(5)$$

The feasible region determined by the constraints is given by



The corner points of the feasible region are $A(20, 80)$, $B(40, 160)$ and $C(20, 180)$.

The values of Z at these corner points are as follows:

Corner point	$Z = 1000x + 600y$	
$A(20, 80)$	68000	
$B(40, 160)$	136000	→ Maximum
$C(20, 180)$	128000	

Thus, the maximum value of Z is 136000 at $B(40, 160)$.

Therefore, 40 tickets of executive class and 160 tickets of economy class should be sold to maximize the profit and the maximum profit is ₹ 136000.

Question 6:

Two godowns A and B have grain capacity of 100 quintals and 50 quintals respectively. They supply to 3 ration shops, D, E and F whose requirements are 60, 50 and 40 quintals respectively. The cost of transportation per quintal from the godowns to the shops are given in the following table:

Transportation cost per quintal (₹/kg)		
From/To	A	B
D	6	4
E	3	2
F	2.50	3

How should the supplies be transported in order that the transportation cost is minimum? What is the minimum cost?

Solution:

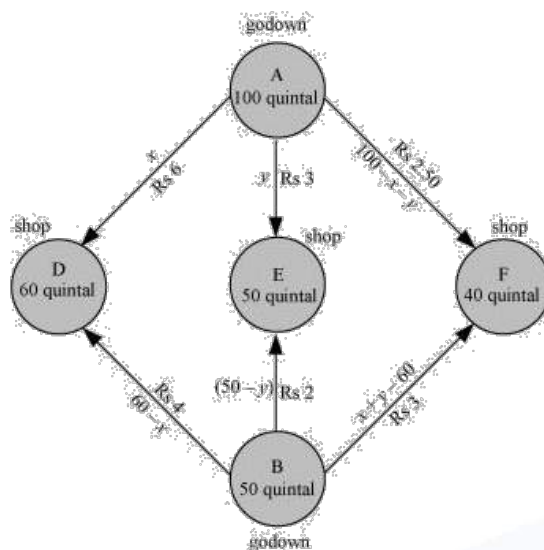
Let godown A supply x and y quintals of grain to the shops D and E, respectively.

Then, $(100 - x - y)$ will be supplied to shop F.

The requirement at shop D is 60 quintals since x quintals are transported from godown A. Therefore, the remaining $(60 - x)$ quintals will be transported from godown B.

Similarly, $(50 - y)$ quintals and $40 - (100 - x - y) = (x + y - 60)$ quintals will be transported from godown B to shop E and F respectively.

The given problem can be represented diagrammatically as follows:



Thus,

$$x \geq 0, y \geq 0 \text{ and } 100 - x - y \geq 0$$

$$\Rightarrow x \geq 0, y \geq 0 \text{ and } x + y \leq 100$$

And

$$60 - x \geq 0, 50 - y \geq 0 \text{ and } x + y - 60 \geq 0$$

$$\Rightarrow x \leq 60, y \leq 50 \text{ and } x + y \geq 60$$

Total transportation cost Z is given by

$$\begin{aligned} Z &= 6x + 3y + 2.5(100 - x - y) + 4(60 - x) + 2(50 - y) + 3(x + y - 60) \\ &= 6x + 3y + 250 - 2.5x - 2.5y + 240 - 4x + 100 - 2y + 3x + 3y - 180 \\ &= 2.5x + 1.5y + 410 \end{aligned}$$

The given problem can be formulated as

Minimize

$$Z = 2.5x + 1.5y + 410 \quad \dots(1)$$

Subject to the constraints,

$$x + y \leq 100 \quad \dots(2)$$

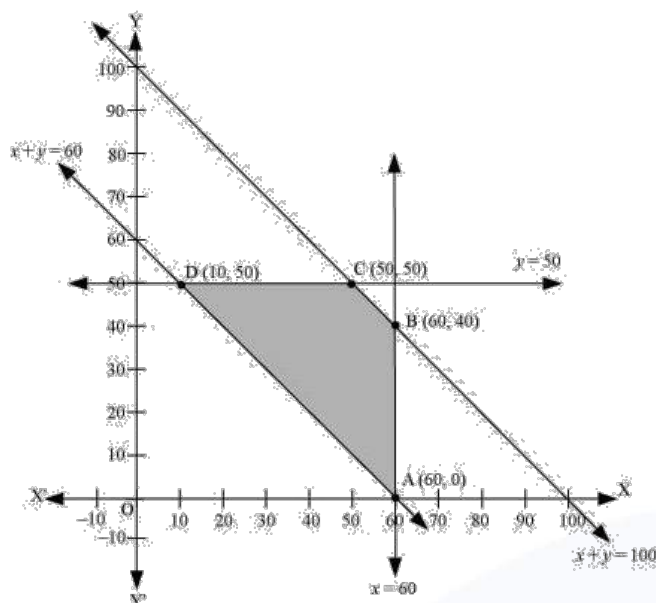
$$x \leq 60 \quad \dots(3)$$

$$y \leq 50 \quad \dots(4)$$

$$x + y \geq 60 \quad \dots(5)$$

$$x, y \geq 0 \quad \dots(6)$$

The feasible region determined by the system of constraints is given by



The corner points are $A(60,0)$, $B(60,40)$, $C(50,50)$ and $D(10,50)$.

The values of Z at these corner points are as follows:

Corner point	$Z = 2.5x + 1.5y + 410$	
$A(60,0)$	560	
$B(60,40)$	620	
$C(50,50)$	610	
$D(10,50)$	510	→ Minimum

Thus, the minimum value of Z is 510 at $D(10,50)$.

Thus, the minimum cost is ₹ 510.

Question 7:

An oil company has two depots A and B with capacities of 7000 L and 4000 L respectively. The company is to supply oil to three petrol pumps, D, E and F whose requirements are 4500L, 3000L and 3500L respectively. The distance (in km) between the depots and the petrol pumps is given in the following table:

Distance (in km)		
From/To	A	B

D	7	3
E	6	4
F	3	2

Assuming that the transportation cost of 10 litres of oil is ₹ 1 per km, how should the delivery be scheduled in order that the transportation cost is minimum? What is the minimum cost?

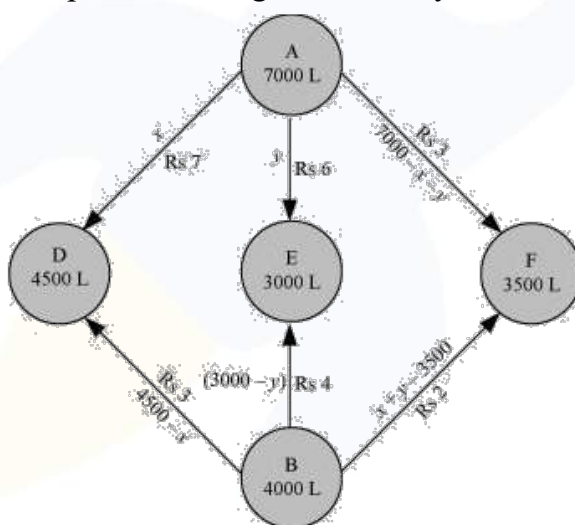
Solution:

Let x and y litres of oil be supplied from A to the petrol pumps, D and E. Then, $(7000 - x - y)$ will be supplied from A to petrol pump F.

The requirement at petrol pump D is 4500 L. Since x L are transported from depot A, the remaining $(4500 - x)$ L will be transported from petrol pump B.

Similarly, $(3000 - y)$ L and $3500 - (7000 - x - y) = (x + y - 3500)$ L will be transported from depot B to petrol pump E and F respectively.

The given problem can be represented diagrammatically as follows:



Thus,

$$x \geq 0, y \geq 0 \text{ and } 7000 - x - y \geq 0$$

$$\Rightarrow x \geq 0, y \geq 0 \text{ and } x + y \leq 7000$$

And

$$4500 - x \geq 0, 3000 - y \geq 0 \text{ and } x + y - 3500 \geq 0$$

$$\Rightarrow x \leq 4500, y \leq 3000 \text{ and } x + y \geq 3500$$

Cost of transporting 10 L of petrol in ₹ = 1

Cost of transporting 1 L of petrol in ₹ = $\frac{1}{10}$

Therefore, total transportation cost is given by,

$$Z = \frac{7}{10}x + \frac{6}{10}y + \frac{3}{10}(7000 - x - y) + \frac{3}{10}(4500 - x) + \frac{4}{10}(3000 - y) + \frac{2}{10}(x + y - 3500)$$

$$= 0.3x + 0.1y + 3950$$

The problem can be formulated as follows.

Minimize

$$Z = 0.3x + 0.1y + 3950 \quad \text{.....(1)}$$

Subject to the constraints,

$$x + y \leq 7000 \quad \text{.....(2)}$$

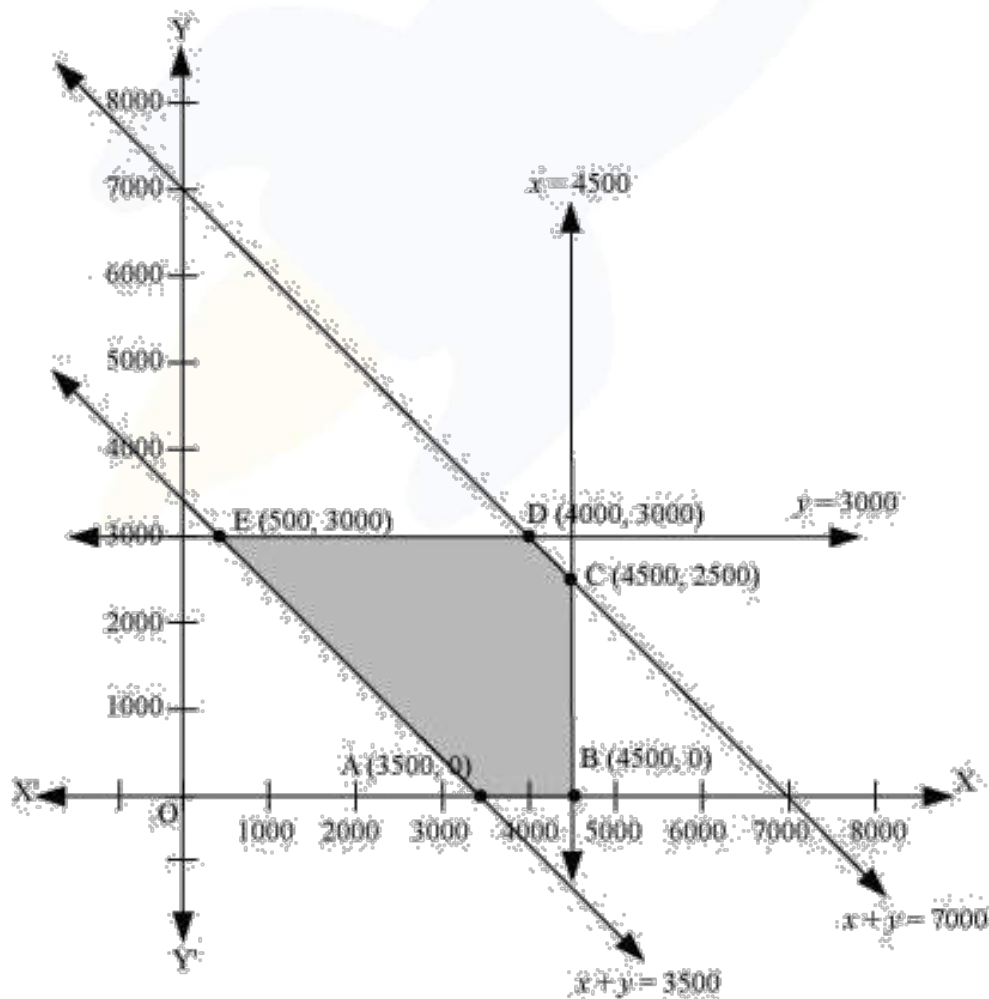
$$x \leq 4500 \quad \text{.....(3)}$$

$$y \leq 3000 \quad \text{.....(4)}$$

$$x + y \geq 3500 \quad \text{.....(5)}$$

$$x, y \geq 0 \quad \text{.....(6)}$$

The feasible region determined by the constraints is given by



The corner points of the feasible region are $A(3500,0)$, $B(4500,0)$, $C(4500,2500)$, $D(4000,3000)$ and $E(500,3000)$.

The values of Z at these corner points are as follows:

Corner point	$Z = 0.3x + 0.1y + 3950$	
$A(3500,0)$	5000	
$B(4500,0)$	5300	
$C(4500,2500)$	5550	
$D(4000,3000)$	5450	
$E(500,3000)$	4400	→ Minimum

Thus, the minimum value of Z is 4400 at $E(500,3000)$.

Therefore, the minimum transportation cost is ₹ 4400.

Question 8:

A fruit grower can use two types of fertilizer in his garden, brand P and brand Q. The amounts (in kg) of nitrogen, phosphoric acid, potash, and chlorine in a bag of each brand are given in the table. Tests indicate that the garden needs at least 240 kg of phosphoric acid at least 270 kg of potash and at most 310 kg of chlorine.

If the grower wants to minimize the amount of nitrogen added to the garden, how many bags of each brand should be used? What is the minimum amount of nitrogen added in the garden?

Kg per bag		
	Brand P	Brand Q
Nitrogen	3	3.5
Phosphoric Acid	1	2
Potash	3	1.5
Chlorine	1.5	2

Solution:

Let the fruit grower use x bags of brand P and y bags of brand Q.
 The problem can be formulated as follows.

Minimize

$$Z = 3x + 3.5y \quad \dots(1)$$

Subject to the constraints,

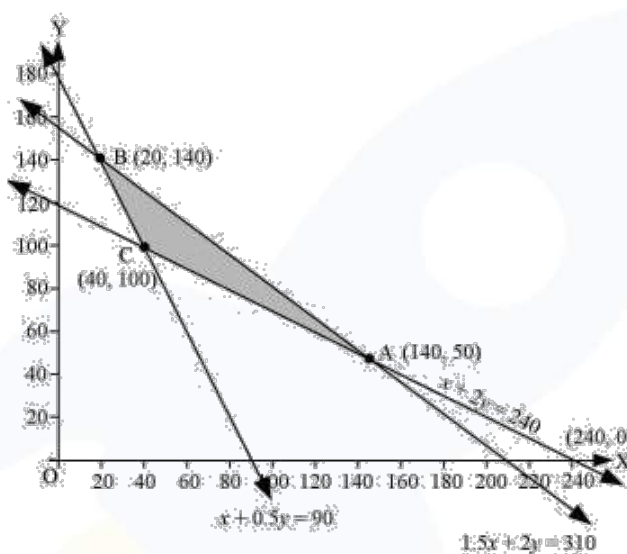
$$x + 2y \geq 240 \quad \dots(2)$$

$$x + 0.5y \geq 90 \quad \dots(3)$$

$$1.5x + 2y \leq 310 \quad \dots(4)$$

$$x, y \geq 0 \quad \dots(5)$$

The feasible region determined by the system of constraints is given by



The corner points are $A(140, 50)$, $B(20, 140)$ and $C(40, 100)$.

The values of Z at these corner points are as follows:

Corner point	$Z = 3x + 3.5y$	
$A(140, 50)$	595	
$B(20, 140)$	550	
$C(40, 100)$	470	→ Minimum

Thus, the minimum value of Z is 470 at $C(40, 100)$.

Therefore, 40 bags of brand P and 100 bags of brand Q should be added to the garden to minimize the amount of nitrogen.

Hence, the minimum amount of nitrogen added to the garden is 470 kg.

Question 9:

Refer to question 8. If the grower wants to maximize the amount of nitrogen added to the garden, how many bags of each brand should be added? What is the maximum amount of nitrogen added?

Solution:

Let the fruit grower use x bags of brand P and y bags of brand Q.
 The problem can be formulated as follows.

Maximize

$$Z = 3x + 3.5y \quad \dots(1)$$

Subject to the constraints,

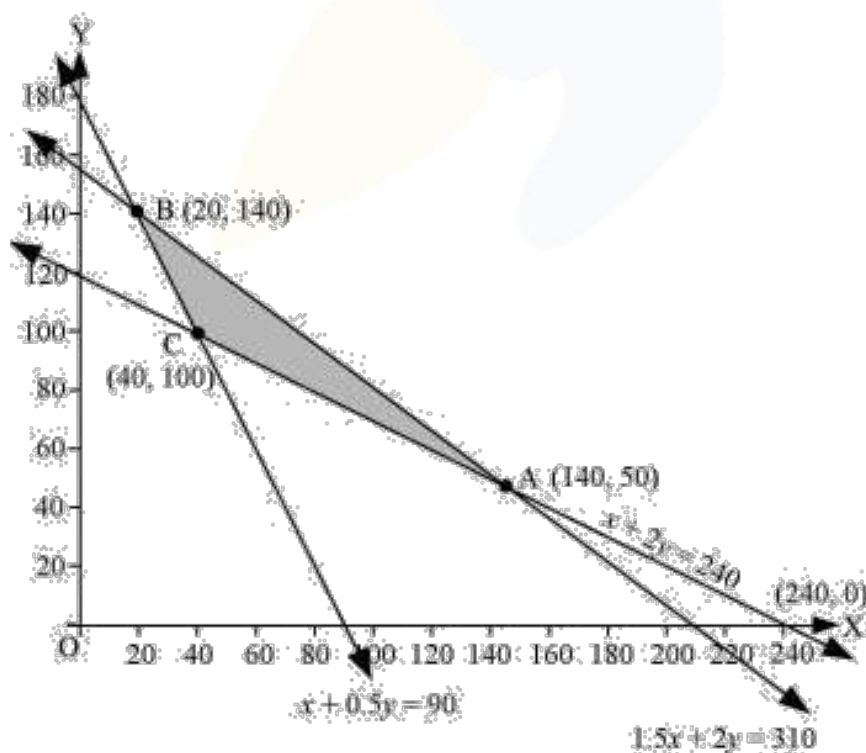
$$x + 2y \geq 240 \quad \dots(2)$$

$$x + 0.5y \geq 90 \quad \dots(3)$$

$$1.5x + 2y \leq 310 \quad \dots(4)$$

$$x, y \geq 0 \quad \dots(5)$$

The feasible region determined by the system of constraints is given by



The corner points are $A(140, 50)$, $B(20, 140)$ and $C(40, 100)$.

The values of Z at these corner points are as follows:

Corner point	$Z = 3x + 3.5y$	
$A(140, 50)$	595	→ Maximum
$B(20, 140)$	550	
$C(40, 100)$	470	

Thus, the maximum value of Z is 595 at $A(140, 50)$.

Hence, 140 bags of brand P and 50 bags of brand Q should be used to maximize the amount of nitrogen.

Thus, the maximum amount of nitrogen added to the garden is 595 kg.

Question 10:

A toy company manufactures two types of dolls, A and B. Market tests and available resources have indicated that the combined production level should not exceed 1200 dolls per week and the demand for dolls of type B is at most half of that for dolls of type A. Further, the production level of dolls of type A can exceed three times the production of dolls of other type by at most 600 units. If the company makes profit of ₹ 12 and ₹ 16 per doll respectively on dolls A and B, how many of each should be produced weekly in order to maximize the profit?

Solution:

Let x and y be the number of dolls of type A and B respectively that are produced per week. The given problem can be formulated as follows.

Maximize

$$Z = 12x + 16y \quad \dots(1)$$

Subject to the constraints,

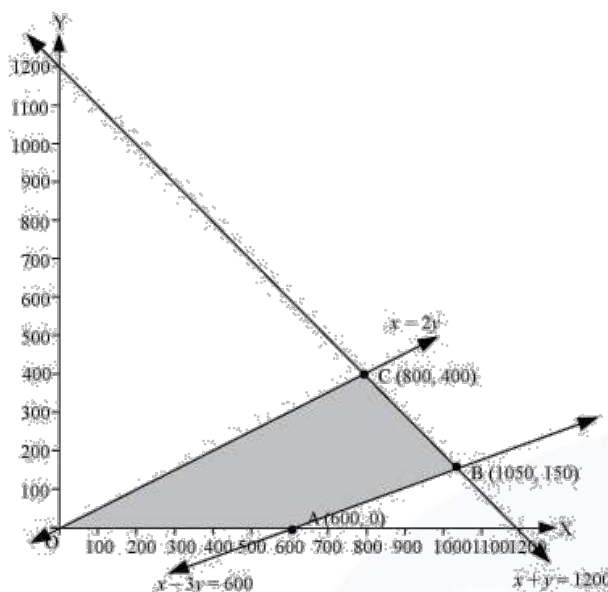
$$x + y \leq 1200 \quad \dots(2)$$

$$y \leq \frac{x}{2} \Rightarrow x \geq 2y \quad \dots(3)$$

$$x - 3y \leq 600 \quad \dots(4)$$

$$x, y \geq 0 \quad \dots(5)$$

The feasible region determined by the system of constraints is given by



The corner points are $A(600, 0)$, $B(1050, 150)$ and $C(800, 400)$.

The values of Z at these corner points are as follows:

Corner point	$Z = 12x + 16y$	
$A(600, 0)$	7200	
$B(1050, 150)$	15000	
$C(800, 400)$	16000	→ Maximum

Thus, the maximum value of Z is 16000 at $(800, 400)$.

Hence, 800 and 400 dolls of type A and type B should be produced respectively to get the maximum profit of ₹ 16000.

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