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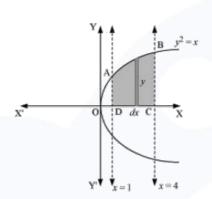


NCERT Solutions Class 12 Maths Chapter 8 Applications of Integrals

Question 1:

Find the area of the region bounded by the curve $y^2 = x$ and the lines x = 1, x = 4 and the x-axis in the first quadrant.

Solution:



$$ar(ABCD) = \int_{1}^{4} y dx$$

$$= \int_{1}^{4} \sqrt{x} dx$$

$$= \left[\frac{x^{\frac{3}{2}}}{\frac{3}{2}} \right]_{1}^{4}$$

$$= \frac{2}{3} \left[(4)^{\frac{3}{2}} - (1)^{\frac{3}{2}} \right]$$

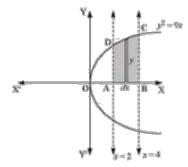
$$= \frac{2}{3} [8 - 1]$$

$$= \frac{14}{3}$$

Question 2:

Find the area of the region bounded by $y^2 - 9x$, x = 2, x = 4 and the x-axis in the first quadrant.





$$ar(ABCD) = \int_{2}^{4} y dx$$

$$= \int_{2}^{4} 3\sqrt{x} dx$$

$$= 3 \left[\frac{x^{\frac{3}{2}}}{\frac{3}{2}} \right]_{2}^{4}$$

$$= 2 \left[x^{\frac{3}{2}} \right]_{2}^{4}$$

$$= 2 \left[(4)^{\frac{3}{2}} - (2)^{\frac{3}{2}} \right]$$

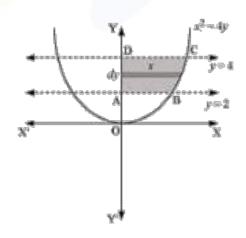
$$= 2 \left[8 - 2\sqrt{2} \right]$$

$$= (16 - 4\sqrt{2})$$

Question 3:

Find the area of the region bounded by $x^2 = 4y$, y = 2, y = 4 and the y-axis in the first quadrant.

Solution:





$$ar(ABCD) = \int_{2}^{4} x dy$$

$$= \int_{2}^{4} 2\sqrt{y} dy = 2\int_{2}^{4} \sqrt{y} dy$$

$$= 2\left[\frac{y^{\frac{3}{2}}}{\frac{3}{2}}\right]_{2}^{4}$$

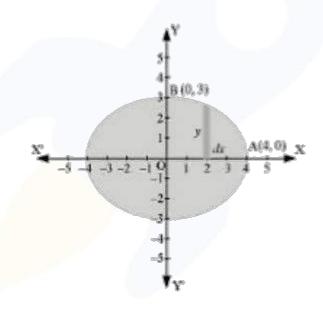
$$= \frac{4}{3}\left[(4)^{\frac{3}{2}} - (2)^{\frac{3}{2}}\right] = \frac{4}{3}\left[8 - 2\sqrt{2}\right]$$

$$= \left(\frac{32 - 8\sqrt{2}}{3}\right)$$

Question 4:

Find the area of the region bounded by the ellipse $\frac{x^2}{16} + \frac{y^2}{9} = 1$.

Solution:



It is given that

$$\Rightarrow \frac{x^2}{16} + \frac{y^2}{9} = 1$$

$$\Rightarrow \frac{y^2}{9} = 1 - \frac{x^2}{16}$$

$$\Rightarrow y = 3\sqrt{1 - \frac{x^2}{16}}$$

Area of ellipse = $4 \times ar(OAB)$



$$ar(OAB) = \int_0^4 y dx$$

$$= \int_0^4 3\sqrt{1 - \frac{x^2}{16}} dx$$

$$= \frac{3}{4} \int_0^4 \sqrt{16 - x^2} dx$$

$$= \frac{3}{4} \left[\frac{x}{2} \sqrt{16 - x^2} + \frac{16}{2} \sin^{-1} \frac{x}{4} \right]_0^4$$

$$= \frac{3}{4} \left[2\sqrt{16 - 16} + 8 \sin^{-1} (1) - 0 - 8 \sin^{-1} (0) \right]$$

$$= \frac{3}{4} \left[\frac{8\pi}{2} \right]$$

$$= \frac{3}{4} [4\pi]$$

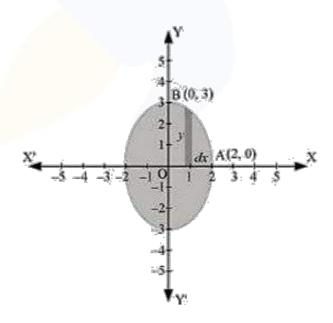
$$= 3\pi$$

Area of ellipse = $4 \times 3\pi = 12\pi$ units

Question 5:

Find the area of the region bounded by the ellipse $\frac{x^2}{4} + \frac{y^2}{9} = 1$

Solution:



It is given that

$$\Rightarrow \frac{x^2}{4} + \frac{y^2}{9} = 1$$
$$\Rightarrow y = 3\sqrt{1 - \frac{x^2}{4}}$$



Area of ellipse =
$$4 \times ar(OAB)$$

$$ar(OAB) = \int_0^2 y dx$$

$$= \int_0^2 3\sqrt{1 - \frac{x^2}{4}} dx$$

$$= \frac{3}{2} \int_0^2 \sqrt{4 - x^2} dx$$

$$= \frac{3}{2} \left[\frac{x}{2} \sqrt{4 - x^2} + \frac{4}{2} \sin^{-1} \frac{x}{2} \right]_0^2$$

$$= \frac{3}{2} \left[\frac{2\pi}{2} \right]$$

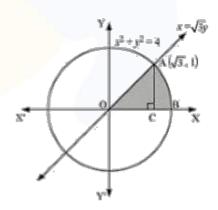
$$= \frac{3\pi}{2}$$

Area of ellipse $= 4 \times \frac{3\pi}{2} = 6\pi$ units.

Question 6:

Find the area of the region in the first quadrant enclosed by x-axis, line $x = \sqrt{3}y$ and the circle $x^2 + y^2 = 4$

Solution:



$$ar(OAB) = ar(\triangle OAC) + ar(ABC)$$

$$ar(\triangle OAC) = \frac{1}{2} \times OC \times AC$$

$$= \frac{1}{2} \times \sqrt{3} \times 1$$

$$= \frac{\sqrt{3}}{2}$$

$$ar(ABC) = \int_{\sqrt{3}}^{2} y dx$$

$$= \int_{\sqrt{3}}^{2} \sqrt{4 - x^{2}} dx$$

$$= \left[\frac{x}{2} \sqrt{4 - x^{2}} + \frac{4}{2} \sin^{-1} \left(\frac{x}{2} \right) \right]_{\sqrt{3}}^{2}$$

$$= \left[2 \times \frac{\pi}{2} - \frac{\sqrt{3}}{2} \sqrt{4 - 3} - 2 \sin^{-1} \left(\frac{\sqrt{3}}{2} \right) \right]$$

$$= \left[\pi - \frac{\sqrt{3}}{2} - 2 \left(\frac{\pi}{3} \right) \right]$$

$$= \left[\pi - \frac{2\pi}{3} - \frac{\sqrt{3}}{2} \right]$$

$$= \left[\frac{3\pi - 2\pi}{3} - \frac{\sqrt{3}}{2} \right]$$

$$= \left[\frac{\pi}{3} - \frac{\sqrt{3}}{2} \right]$$

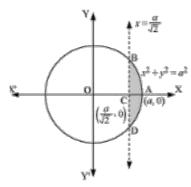
Therefore, required area enclosed $=\frac{\sqrt{3}}{2} + \frac{\pi}{3} - \frac{\sqrt{3}}{2} = \frac{\pi}{3}$ square units.

Question 7:

Find the area of the smaller part of the circle $x^2 + y^2 = a^2$ cut off by the line $x = \frac{a}{\sqrt{2}}$.

Solution:

The area of the smaller part of the circle, $x^2 + y^2 = a^2$ cut off by the line, $x = \frac{a}{\sqrt{2}}$, is the area ABCD.



It can be observed that the area ABCD is symmetrical about *x*-axis.



$$ar(ABCD) = 2 \times ar(ABC)$$

$$ar(ABC) = \int_{\frac{a}{\sqrt{2}}}^{a} y dx$$

$$= \int_{\frac{a}{\sqrt{2}}}^{a} \sqrt{a^{2} - x^{2}} dx$$

$$= \left[\frac{x}{2} \sqrt{a^{2} - x^{2}} + \frac{a^{2}}{2} \sin^{-1} \left(\frac{x}{a} \right) \right]_{\frac{a}{\sqrt{2}}}^{a}$$

$$= \left[\frac{a^{2}}{2} \left(\frac{\pi}{2} \right) - \frac{a}{2\sqrt{2}} \sqrt{a^{2} - \frac{a^{2}}{2}} - \frac{a^{2}}{2} \sin^{-1} \left(\frac{1}{\sqrt{2}} \right) \right]$$

$$= \frac{a^{2}\pi}{4} - \frac{a}{2\sqrt{2}} \cdot \frac{a}{\sqrt{2}} - \frac{a^{2}}{2} \left(\frac{\pi}{4} \right)$$

$$= \frac{a^{2}\pi}{4} - \frac{a^{2}}{4} - \frac{a^{2}\pi}{8}$$

$$= \frac{a^{2}}{4} \left[\pi - 1 - \frac{\pi}{2} \right]$$

$$= \frac{a^{2}}{4} \left[\frac{\pi}{2} - 1 \right]$$

$$ar(ABCD) = 2\left[\frac{a^2}{4}\left(\frac{\pi}{2} - 1\right)\right]$$
$$= \frac{a^2}{2}\left(\frac{\pi}{2} - 1\right)$$

Therefore, the required area is $\frac{a^2}{2} \left(\frac{\pi}{2} - 1 \right)$ square units.

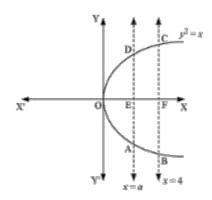
Question 8:

The area between $x = y^2$ and x = 4 is divided into two equal parts by the line x = a, find the value of a.

Solution:

The line x = a divides the area bounded by the parabola and x = 4 into two equal parts. Therefore, ar(OAD) = ar(ABCD)





It can be observed that the given area is symmetrical about *x*-axis.

Hence,
$$ar(OED) = ar(EFCD)$$

$$ar(OED) = \int_0^a y dx$$

$$= \int_0^a \sqrt{x} dx$$

$$= \left[\frac{\frac{3}{2}}{\frac{3}{2}}\right]_0^a$$

$$= \frac{2}{3}a^{\frac{3}{2}} \qquad \dots (1)$$

$$ar(EFCD) = \int_{a}^{4} \sqrt{x} dx$$

$$= \left[\frac{x^{\frac{3}{2}}}{\frac{3}{2}}\right]_{a}^{4}$$

$$= \frac{2}{3} \left[8 - a^{\frac{3}{2}}\right] \qquad \dots (2)$$



From (1) and (2), we obtain

$$\Rightarrow \frac{2}{3}(a)^{\frac{3}{2}} = \frac{2}{3} \left[8 - (a)^{\frac{3}{2}} \right]$$

$$\Rightarrow 2(a)^{\frac{3}{2}} = 8$$

$$\Rightarrow (a)^{\frac{3}{2}} = 4$$

$$\Rightarrow a = (4)^{\frac{2}{3}}$$

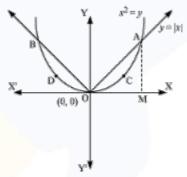
Therefore, the value of $a = (4)^{\frac{2}{3}}$.

Question 9:

Find the area of the region bounded by the parabola $y = x^2$ and the line y = |x|.

Solution:

The area bounded by the parabola $y = x^2$ and the line y = |x|, can be represented as



The given area is symmetrical about *y*-axis.

Therefore,
$$ar(OACO) = ar(ODBO)$$

The point of intersection of parabola $y = x^2$ and the line y = |x|, is A(1,1).

$$ar(OACO) = ar(\Delta OAM) - ar(OMACO)$$

$$ar(\Delta OAM) = \frac{1}{2} \times OM \times AM$$
$$= \frac{1}{2} \times 1 \times 1$$
$$= \frac{1}{2}$$

$$ar(OMACO) = \int_0^1 y dx$$
$$= \int_0^1 x^2 dx$$
$$= \left[\frac{x^3}{3}\right]_0^1$$
$$= \frac{1}{3}$$

$$ar(OACO) = ar(\Delta OAM) - ar(OMACO)$$

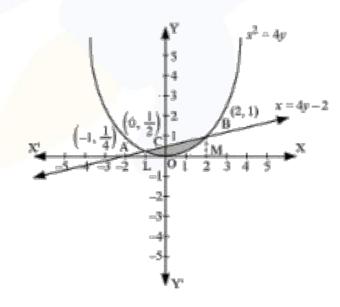
= $\frac{1}{2} - \frac{1}{3}$
= $\frac{1}{6}$

Therefore, the required area $=2\left[\frac{1}{6}\right] = \frac{1}{3}$ units.

Question 10:

Find the area bounded by the curve $x^2 = 4y$ and the line x = 4y - 2.

Solution:



Coordinates of point $A\left(-1,\frac{1}{4}\right)$.

Coordinates of point B(2,1).



Draw AL and BM perpendicular to x-axis.

$$ar(OBAO) = ar(OBCO) + ar(OACO)$$

$$ar(OBCO) = ar(OMBC) - ar(OMBO)$$

$$= \int_0^2 \frac{x+2}{4} dx - \int_0^2 \frac{x^2}{4} dx$$

$$= \frac{1}{4} \left[\frac{x^2}{2} + 2x \right]_0^2 - \frac{1}{4} \left[\frac{x^3}{3} \right]_0^2$$

$$= \frac{1}{4} [2+4] - \frac{1}{4} \left[\frac{8}{3} \right]$$

$$= \frac{3}{2} - \frac{2}{3}$$

$$= \frac{5}{6}$$

$$ar(OACO) = ar(OLAC) - ar(OLAO)$$

$$= \int_{-1}^{0} \frac{x+2}{4} dx - \int_{-1}^{0} \frac{x^{2}}{4} dx$$

$$= \frac{1}{4} \left[\frac{x^{2}}{2} + 2x \right]_{-1}^{0} - \frac{1}{4} \left[\frac{x^{3}}{3} \right]_{-1}^{0}$$

$$= -\frac{1}{4} \left[\frac{(-1)^{2}}{2} + 2(-1) \right] - \left[-\frac{1}{4} \left(\frac{(-1)^{3}}{3} \right) \right]$$

$$= -\frac{1}{4} \left[\frac{1}{2} - 2 \right] - \frac{1}{12}$$

$$= -\frac{1}{8} + \frac{1}{2} - \frac{1}{12}$$

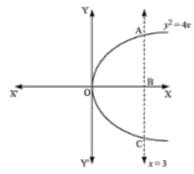
$$= \frac{7}{24}$$

Required area
$$=$$
 $\left(\frac{5}{6} + \frac{7}{24}\right) = \frac{9}{8}$ units.

Question 11:

Find the area of the region bounded by the curve $y^2 = 4x$ and the line x = 3.





OACO is symmetrical about *x*-axis.

Therefore, $ar(OACO) = 2 \times ar(AOB)$

ar(OACO) =
$$2\left[\int_0^3 y dx\right]$$

= $2\left[\int_0^3 2\sqrt{x} dx\right]$
= $4\left[\frac{x^{\frac{3}{2}}}{\frac{3}{2}}\right]_0^3$
= $\frac{8}{3}\left[\left(3\right)^{\frac{3}{2}}\right]$
= $8\sqrt{3}$

Required area is $8\sqrt{3}$ units.

Question 12:

Area lying in the first quadrant and bounded by the circle $x^2 + y^2 = 4$ and the lines x = 0 and x = 2 is

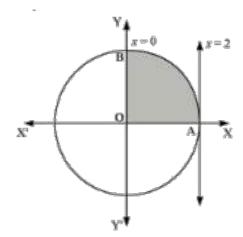
(A) π

(B) $\frac{\pi}{2}$

(C) $\frac{\pi}{3}$

(D) $\frac{\pi}{4}$





$$ar(OAB) = \int_0^2 y dx$$

$$= \int_0^2 \sqrt{4 - x^2} dx$$

$$= \left[\frac{x}{2} \sqrt{4 - x^2} + \frac{4}{2} \sin^{-1} \frac{x}{2} \right]_0^2$$

$$= 2\left(\frac{\pi}{2} \right)$$

$$= \pi$$

Correct answer is A.



Question 13:

Area of the region bounded by the curve $y^2 = 4x$, y-axis and the line y = 3 is

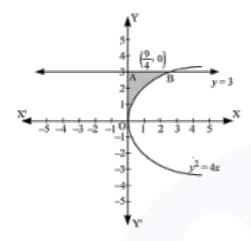
(A) ²

(B) $\frac{9}{4}$

(C) $\frac{9}{3}$

(D) $\frac{9}{2}$

Solution:



$$ar(OAB) = \int_0^3 x dy$$
$$= \int_0^3 \frac{y^2}{4} dy$$
$$= \frac{1}{4} \left[\frac{y^3}{3} \right]_0^3$$
$$= \frac{1}{12} (27)$$
$$= \frac{9}{4}$$

Correct answer is B.

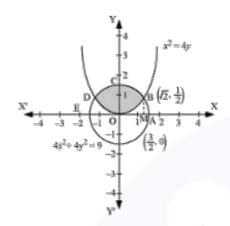


EXERCISE 8.2

Question 1:

Find the area of the circle $4x^2 + 4y^2 = 9$ which is interior to the parabola $x^2 = 4y$.

Solution:



Solving $4x^2 + 4y^2 = 9$ and $x^2 = 4y$, point of intersection $B\left(\sqrt{2}, \frac{1}{2}\right)$ and $D\left(-\sqrt{2}, \frac{1}{2}\right)$. Required area is symmetrical about y-axis.

$$ar(OBCDO) = 2 \times ar(OBCO)$$

Draw BM perpendicular to OA

Coordinates of M are $(\sqrt{2},0)$

$$ar(OBCO) = ar(OMBCO) - ar(OMBO)$$

$$= \int_0^{\sqrt{2}} \sqrt{\frac{9 - 4x^2}{4}} dx - \int_0^{\sqrt{2}} \frac{x^2}{4} dx$$

$$= \frac{1}{2} \int_0^{\sqrt{2}} \sqrt{9 - 4x^2} dx - \frac{1}{4} \int_0^{\sqrt{2}} x^2 dx$$

$$= \frac{1}{4} \left[x\sqrt{9 - 4x^2} + \frac{9}{2} \sin^{-1} \frac{2x}{3} \right]_0^{\sqrt{2}} - \frac{1}{4} \left[\frac{x^3}{3} \right]_0^{\sqrt{2}}$$

$$= \frac{1}{4} \left[\sqrt{2} \sqrt{9 - 8} + \frac{9}{2} \sin^{-1} \frac{2\sqrt{2}}{3} \right] - \frac{1}{12} \left(\sqrt{2} \right)^3$$

$$= \frac{\sqrt{2}}{4} + \frac{9}{8} \sin^{-1} \frac{2\sqrt{2}}{3} - \frac{\sqrt{2}}{6}$$

$$= \frac{\sqrt{2}}{12} + \frac{9}{8} \sin^{-1} \frac{2\sqrt{2}}{3}$$

$$= \frac{1}{4} \left(\frac{\sqrt{2}}{3} + \frac{9}{2} \sin^{-1} \frac{2\sqrt{2}}{3} \right)$$



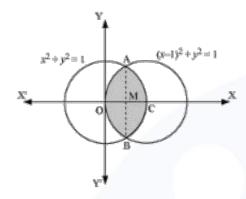
Required area OBCDO

$$= \left(2 \times \frac{1}{4} \left[\frac{\sqrt{2}}{3} + \frac{9}{2} \sin^{-1} \frac{2\sqrt{2}}{3} \right] \right) = \left[\frac{\sqrt{2}}{6} + \frac{9}{4} \sin^{-1} \frac{2\sqrt{2}}{3} \right] \text{ units.}$$

Question 2:

Find the area bounded by curves $(x-1)^2 + y^2 = 1$ and $x^2 + y^2 = 1$.

Solution:



Solving $(x-1)^2 + y^2 = 1$ and $x^2 + y^2 = 1$, point of intersection $A\left(\frac{1}{2}, \frac{\sqrt{3}}{2}\right)$ and $B\left(\frac{1}{2}, -\frac{\sqrt{3}}{2}\right)$ Required area is symmetrical about x-axis.

$$ar(OBCAO) = 2 \times ar(OCAO)$$

Join AB, intersects OC at M

AM is perpendicular to OC

Coordinates of
$$M\left(\frac{1}{2},0\right)$$



$$ar(OCAO) = ar(OMAO) + ar(MCAM)$$

$$= \left[\int_{0}^{\frac{1}{2}} \sqrt{1 - (x - 1)^{2}} \, dx + \int_{\frac{1}{2}}^{1} \sqrt{1 - x^{2}} \, dx \right]$$

$$= \left[\frac{x - 1}{2} \sqrt{1 - (x - 1)^{2}} + \frac{1}{2} \sin^{-1}(x - 1) \right]_{0}^{\frac{1}{2}} + \left[\frac{x}{2} \sqrt{1 - x^{2}} + \frac{1}{2} \sin^{-1}x \right]_{\frac{1}{2}}^{1}$$

$$= \left[-\frac{1}{4} \sqrt{1 - \left(\frac{1}{2}\right)^{2}} + \frac{1}{2} \sin^{-1}\left(\frac{1}{2} - 1\right) - \frac{1}{2} \sin^{-1}(-1) \right] + \left[+\frac{1}{2} \sin^{-1}(-1) - \frac{1}{4} \sqrt{1 - \left(\frac{1}{2}\right)^{2}} - \frac{1}{2} \sin^{-1}\left(\frac{1}{2}\right) \right]$$

$$= \left[-\frac{\sqrt{3}}{8} + \frac{1}{2} \left(-\frac{\pi}{6} \right) - \frac{1}{2} \left(-\frac{\pi}{2} \right) \right] + \left[\frac{1}{2} \left(\frac{\pi}{2} \right) - \frac{\sqrt{3}}{8} - \frac{1}{2} \left(\frac{\pi}{6} \right) \right]$$

$$= \left[-\frac{\sqrt{3}}{4} - \frac{\pi}{12} + \frac{\pi}{4} + \frac{\pi}{4} - \frac{\pi}{12} \right]$$

$$= \left[-\frac{\sqrt{3}}{4} - \frac{\pi}{6} + \frac{\pi}{2} \right]$$

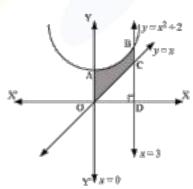
$$= \left[\frac{2\pi}{6} - \frac{\sqrt{3}}{4} \right]$$

Required Area OBCAO is

$$\left(2 \times \left[\frac{2\pi}{6} - \frac{\sqrt{3}}{4}\right]\right) = \left[\frac{2\pi}{3} - \frac{\sqrt{3}}{2}\right] \text{ units.}$$

Question 3:

Find the area of the region bounded by the curves $y = x^2 + 2$, y = x, x = 0 and x = 3 Solution:





$$ar(OCBAO) = ar(ODBAO) - ar(ODCO)$$

$$= \int_0^3 (x^2 + 2) dx - \int_0^3 x dx$$

$$= \left[\frac{x^3}{3} + 2x\right]_0^3 - \left[\frac{x^2}{2}\right]_0^3$$

$$= \left[9 + 6\right] - \left[\frac{9}{2}\right]$$

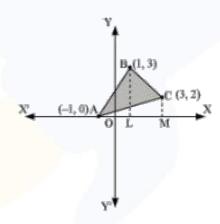
$$= 15 - \frac{9}{2}$$

$$= \frac{21}{2}$$

Question 4:

Using integration finds the area of the region bounded by the triangle whose vertices are (-1,0),(1,3) and (3,2).

Solution:



BL and CM are perpendicular to *x*-axis.

$$ar(\Delta ACB) = ar(ALBA) + ar(BLMCB) - ar(AMCA)$$

Equation of AB is

$$y-0 = \frac{3-0}{1+1}(x+1)$$
$$y = \frac{3}{2}(x+1)$$



$$ar(ALBA) = \int_{-1}^{1} \frac{3}{2}(x+1)dx$$
$$= \frac{3}{2} \left[\frac{x^2}{2} + x \right]_{-1}^{1}$$
$$= \frac{3}{2} \left[\frac{1}{2} + 1 - \frac{1}{2} + 1 \right]$$
$$= 3$$

Equation of BC is

$$y-3 = \frac{2-3}{3-1}(x-1)$$

$$y = \frac{1}{2}(-x+7)$$

$$ar(BLMCB) = \int_{1}^{3} \frac{1}{2}(-x+7)dx$$

$$= \frac{1}{2} \left[-\frac{x^{2}}{2} + 7x \right]_{1}^{3}$$

$$= \frac{1}{2} \left[-\frac{9}{2} + 21 + \frac{1}{2} - 7 \right]$$

$$= 5$$

Equation of AC is

$$y - 0 = \frac{2 - 0}{3 + 1}(x + 1)$$

$$y = \frac{1}{2}(x + 1)$$

$$ar(AMCA) = \frac{1}{2} \int_{-1}^{3} (x + 1) dx$$

$$= \frac{1}{2} \left[\frac{x^2}{2} + x \right]_{-1}^{3}$$

$$= \frac{1}{2} \left[\frac{9}{2} + 3 - \frac{1}{2} + 1 \right]$$

$$= 4$$

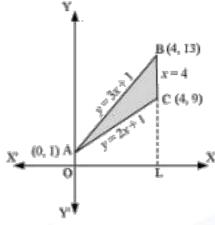
Therefore, $ar(\Delta ABC) = (3+5-4) = 4units$

Question 5:

Using integration find the area of the triangular region whose sides have the equations y = 2x + 1, y = 3x + 1 and x = 4.



Vertices of triangle are A(0,1), B(4,13) and C(4,9).



$$ar(\Delta ACB) = ar(OLBAO) - ar(OLCAO)$$

$$= \int_0^4 (3x+1) dx - \int_0^4 (2x+1) dx$$

$$= \left[\frac{3x^2}{2} + x\right]_0^4 - \left[\frac{2x^2}{2} + x\right]_0^4$$

$$= (24+4) - (16+4)$$

$$= 28 - 20$$

$$= 8$$

Question 6:

Smaller area enclosed by the circle $x^2 + y^2 = 4$ and the line x + y = 2 is

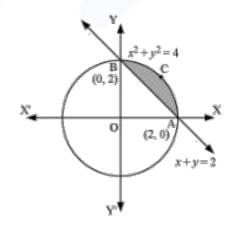
(A)
$$2(\pi-2)$$

(B)
$$\pi - 2$$

(C)
$$2\pi - 1$$

(D)
$$2(\pi+2)$$

Solution:





$$ar(ACBA) = ar(OACBO) - ar(\Delta OAB)$$

$$= \int_0^2 \sqrt{4 - x^2} dx - \int_0^2 (2 - x) dx$$

$$= \left[\frac{x}{2} \sqrt{4 - x^2} + \frac{4}{2} \sin^{-1} \frac{x}{2} \right]_0^2 - \left[2x - \frac{x^2}{2} \right]_0^2$$

$$= \left[2 \times \frac{\pi}{2} \right] - \left[4 - 2 \right]$$

$$= (\pi - 2)$$

Correct answer is B.

Question 7:

Area lying between the curve $y^2 = 4x$ and y = 2x is

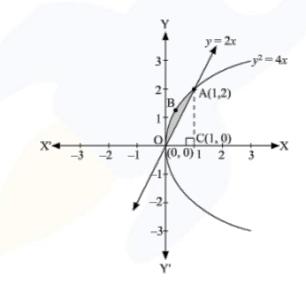
(A)
$$\frac{2}{3}$$

(B)
$$\frac{1}{3}$$

(B)
$$\frac{1}{3}$$
 (C) $\frac{1}{4}$

(D)
$$\frac{3}{4}$$

Solution:



Points of intersection of curve $y^2 = 4x$ and y = 2x are O(0,0) and A(1,2).

Draw AC perpendicular to x-axis.

Coordinates of C are (1,0)



$$ar(OBAO) = ar(\Delta OCA) - ar(OCABO)$$

$$= \int_0^1 2x dx - \int_0^1 2\sqrt{x} dx$$

$$= 2\left[\frac{x^2}{2}\right]_0^1 - 2\left[\frac{x^{\frac{3}{2}}}{\frac{3}{2}}\right]_0^1$$

$$= \left|1 - \frac{4}{3}\right|$$

$$= \left|-\frac{1}{3}\right|$$

$$= \frac{1}{3}$$

Correct answer is B.



MISCELLANEOUS EXERCISE

Question 1:

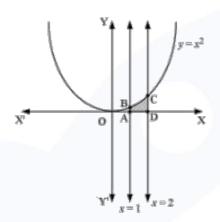
Find the area under the given curves and given lines:

(i)
$$y = x^2, x = 1, x = 2$$
 and x-axis

(ii)
$$y = x^4, x = 1, x = 5 \text{ and } x\text{-axis}$$

Solution:

(i)
$$y = x^2, x = 1, x = 2$$
 and x-axis



$$ar(ADCBA) = \int_{1}^{2} y dx$$

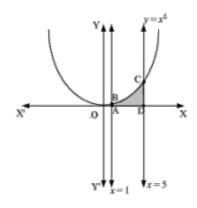
$$= \int_{1}^{2} x^{2} dx$$

$$= \left[\frac{x^{3}}{3}\right]_{1}^{2}$$

$$= \frac{8}{3} - \frac{1}{3}$$

$$= \frac{7}{3}$$

(ii)
$$y = x^4, x = 1, x = 5 \text{ and } x\text{-axis}$$





$$ar(ADCBA) = \int_{1}^{5} y dx$$

$$= \int_{1}^{5} x^{4} dx$$

$$= \left[\frac{x^{5}}{5}\right]_{1}^{5}$$

$$= \frac{(5)^{5}}{5} - \frac{1}{5}$$

$$= (5)^{4} - \frac{1}{5}$$

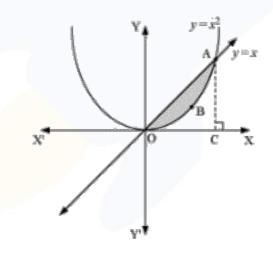
$$= 625 - \frac{1}{5}$$

$$= 624.8$$

Question 2:

Find the area between the curves y = x and $y = x^2$.

Solution:



Point of intersection of y = x and $y = x^2$ is A (1,1).

Draw AC perpendicular to x-axis.



$$ar(OBAO) = ar(\triangle OCA) - ar(OCABO)$$

$$= \int_0^1 x dx - \int_0^1 x^2 dx$$

$$= \left[\frac{x^2}{2}\right]_0^1 - \left[\frac{x^3}{3}\right]_0^1$$

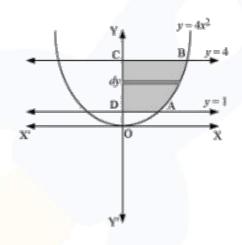
$$= \frac{1}{2} - \frac{1}{3}$$

$$= \frac{1}{6}$$

Question 3:

Find the area of the region lying in the first quadrant and bounded by $y = 4x^2$, x = 0, y = 1 and y = 4.

Solution:



$$ar(ABCD) = \int_{1}^{4} x dy$$

$$= \int_{1}^{4} \frac{\sqrt{y}}{2} dy$$

$$= \frac{1}{2} \left[\frac{y^{\frac{3}{2}}}{\frac{3}{2}} \right]_{1}^{4}$$

$$= \frac{1}{3} \left[(4)^{\frac{3}{2}} - 1 \right]$$

$$= \frac{1}{3} [8 - 1]$$

$$= \frac{7}{3}$$

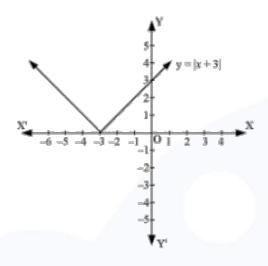


Question 4:

Sketch the graph of y = |x+3| and evaluate $\int_{-6}^{0} |x+3| dx$.

Solution:

X							
Y	3	2	1	0	1	2	3



$$(x+3) \le 0 \text{ for } -6 \le x \le -3 \text{ and } (x+3) \ge 0 \text{ for } -3 \le x \le 0$$

$$\int_{-6}^{0} |(x+3)| dx = -\int_{-6}^{-3} (x+3) dx + \int_{-3}^{0} (x+3) dx$$

$$= -\left[\frac{x^{2}}{2} + 3x \right]_{-6}^{-3} + \left[\frac{x^{2}}{2} + 3x \right]_{-3}^{0}$$

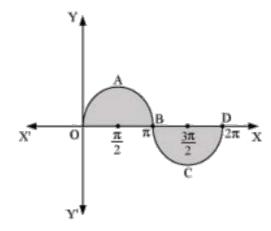
$$= -\left[\left(\frac{(-3)^{2}}{2} + 3(-3) \right) - \left(\frac{(-6)^{2}}{2} + 3(-6) \right) \right] + \left[0 - \left(\frac{(-3)^{2}}{2} + 3(-3) \right) \right]$$

$$= -\left[-\frac{9}{2} \right] - \left[-\frac{9}{2} \right]$$

Question 5:

Find the area bounded by the curve $y = \sin x$ between x = 0 and $x = 2\pi$.





Area bounded by the curve = Area OABO + Area BCDB

$$ar(OABO) + ar(BCDB) = \int_0^{\pi} \sin x dx + \left| \int_{\pi}^{2\pi} \sin x dx \right|$$

$$= \left[-\cos x \right]_0^{\pi} + \left| \left[-\cos x \right]_{\pi}^{2\pi} \right|$$

$$= \left[-\cos \pi + \cos 0 \right] + \left| -\cos 2\pi + \cos \pi \right|$$

$$= 1 + 1 + \left| (-1 - 1) \right|$$

$$= 2 + \left| -2 \right|$$

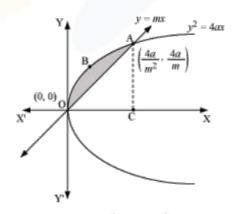
$$= 2 + 2$$

$$= 4$$

Question 6:

Find the area enclosed between the parabola $y^2 = 4ax$ and the line y = mx.

Solution:



Points of intersection of curves are (0,0) and $\left(\frac{4a}{m^2}, \frac{4a}{m}\right)$ Draw AC perpendicular to x-axis.



$$ar(OABO) = ar(OCABO) - ar(\triangle OCA)$$

$$= \int_{0}^{\frac{4a}{m^{2}}} 2\sqrt{ax}dx - \int_{0}^{\frac{4a}{m^{2}}} mxdx$$

$$= 2\sqrt{a} \left[\frac{x^{\frac{3}{2}}}{\frac{3}{2}} \right]_{0}^{\frac{4a}{m^{2}}} - m \left[\frac{x^{2}}{2} \right]_{0}^{\frac{4a}{m^{2}}}$$

$$= \frac{4}{3}\sqrt{a} \left(\frac{4a}{m^{2}} \right)^{\frac{3}{2}} - \frac{m}{2} \left[\left(\frac{4a}{m^{2}} \right)^{2} \right]$$

$$= \frac{32a^{2}}{3m^{3}} - \frac{m}{2} \left(\frac{16a^{2}}{m^{4}} \right)$$

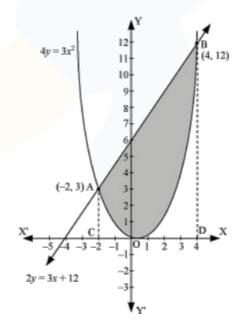
$$= \frac{32a^{2}}{3m^{3}} - \frac{8a^{2}}{m^{3}}$$

$$= \frac{8a^{2}}{3m^{3}}$$

Question 7:

Find the area enclosed by the parabola $4y = 3x^2$ and the line 2y = 3x + 12.

Solution:



Points of intersection of curves are A(-2,3) and B(4,12). Draw AC and BD perpendicular to x-axis.



$$ar(OBAO) = ar(CDBA) - ar(ODBO + OACO)$$

$$= \int_{-2}^{4} \frac{1}{2} (3x + 12) dx - \int_{-2}^{4} \frac{3x^{2}}{4} dx$$

$$= \frac{1}{2} \left[\frac{3x^{2}}{2} + 12x \right]_{-2}^{4} - \frac{3}{4} \left[\frac{x^{3}}{3} \right]_{-2}^{4}$$

$$= \frac{1}{2} [24 + 48 - 6 + 24] - \frac{1}{4} [64 + 8]$$

$$= \frac{1}{2} [90] - \frac{1}{4} [72]$$

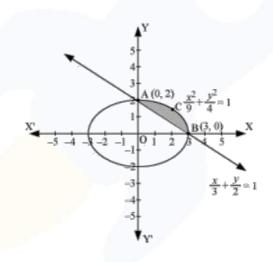
$$= 45 - 18$$

$$= 27$$

Question 8:

Find the area of the smaller region bounded by the ellipse $\frac{x^2}{9} + \frac{y^2}{4} = 1$ and the line $\frac{x}{3} + \frac{y}{2} = 1$.

Solution:





$$ar(BCAB) = ar(OBCAO) - ar(OBAO)$$

$$= \int_0^3 2\sqrt{1 - \frac{x^2}{9}} dx - \int_0^3 2\left(1 - \frac{x}{3}\right) dx$$

$$= \frac{2}{3} \left[\int_0^3 \sqrt{9 - x^2} dx\right] - \frac{2}{3} \int_0^3 (3 - x) dx$$

$$= \frac{2}{3} \left[\frac{x}{2}\sqrt{9 - x^2} + \frac{9}{2}\sin^{-1}\frac{x}{3}\right]_0^3 - \frac{2}{3} \left[3x - \frac{x^2}{2}\right]_0^3$$

$$= \frac{2}{3} \left[\frac{9}{2} \left(\frac{\pi}{2}\right)\right] - \frac{2}{3} \left[9 - \frac{9}{2}\right]$$

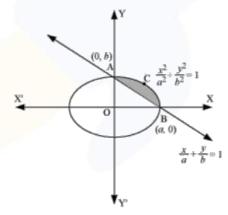
$$= \frac{2}{3} \left[\frac{9\pi}{4} - \frac{9}{2}\right]$$

$$= \frac{2}{3} \times \frac{9}{4} (\pi - 2)$$

$$= \frac{3}{2} (\pi - 2)$$

Question 9:

Find the area of the smaller region bounded by the ellipse $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ and the line $\frac{x}{a} + \frac{y}{b} = 1$. Solution:





$$ar(CBA) = ar(OBCAO) - ar(OBAO)$$

$$= \int_0^a b \sqrt{1 - \frac{x^2}{a^2}} dx - \int_0^a b \left(1 - \frac{x}{a}\right) dx$$

$$= \frac{b}{a} \left[\left\{ \frac{x}{2} \sqrt{a^2 - x^2} + \frac{a^2}{2} \sin^{-1} \frac{x}{a} \right\}_0^a - \left\{ ax - \frac{x^2}{2} \right\}_0^a \right]$$

$$= \frac{b}{a} \left[\left\{ \frac{a^2}{2} \left(\frac{\pi}{2} \right) \right\} - \left\{ a^2 - \frac{a^2}{2} \right\} \right]$$

$$= \frac{b}{a} \left[\frac{a^2 \pi}{4} - \frac{a^2}{2} \right]$$

$$= \frac{ba^2}{2a} \left[\frac{\pi}{2} - 1 \right]$$

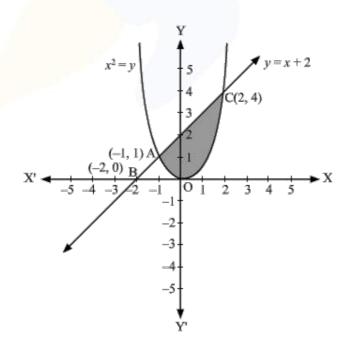
$$= \frac{ab}{4} (\pi - 2)$$

Question 10:

Find the area of the region enclosed by the parabola $x^2 = y$, the line y = x + 2 and x-axis.

Solution:

Point of intersection of $x^2 = y$ and y = x + 2, is A(-1,1) and C(2,4).





Now required Area = Area of trapezium ALMB- Area of ALODBM

$$ar(trap.ALMB) - ar(ALODBM) = \int_{-1}^{2} (x+2) dx - \int_{-1}^{2} x^{2} dx$$

$$= \left[\frac{x^{2}}{2} + 2x \right]_{-1}^{2} - \left[\frac{x^{3}}{3} \right]_{-1}^{2}$$

$$= \left[2 + 4 - \frac{1}{2} + 2 \right] - \left[\frac{8}{3} + \frac{1}{3} \right]$$

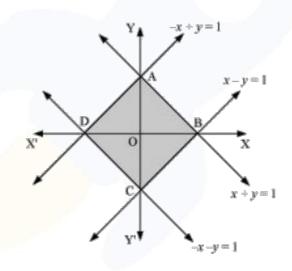
$$= \frac{15}{2} - 3$$

$$= \frac{9}{2}$$

Question 11:

Using the method of integration find the area bounded by the curve |x|+|y|=1[Hint: The required region is bounded by lines x+y=1, x-y=1, -x+y=1 and -x-y=1]

Solution:



Curve intersects axis at points A(0,1), B(1,0), C(0,-1) and D(-1,0).

Curve is symmetrical about *x*-axis and *y*-axis.

$$ar(ADCB) = 4 \times ar(OBAO)$$

$$= 4 \int_0^1 (1 - x) dx$$

$$= 4 \left(x - \frac{x^2}{2} \right)_0^1$$

$$= 4 \left[1 - \frac{1}{2} \right]$$

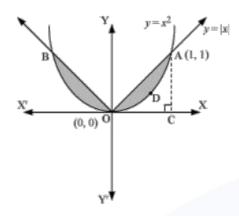
$$= 2$$



Question 12:

Find the area bounded by curves $\{(x, y): y \ge x^2 \text{ and } y = |x|\}$

Solution:



Required area is symmetrical about *y*-axis.

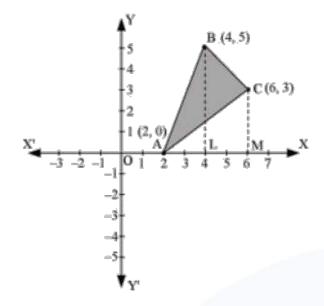
Required area = 2[Area (OCAO) - Area (OCADO)]

$$2\left[ar(OCAO) - ar(OCADO)\right] = 2\left[\int_0^1 x dx - \int_0^1 x^2 dx\right]$$
$$= 2\left[\left[\frac{x^2}{2}\right]_0^1 - \left[\frac{x^3}{3}\right]_0^1\right]$$
$$= 2\left[\frac{1}{2} - \frac{1}{3}\right]$$
$$= 2\left[\frac{1}{6}\right]$$
$$= \frac{1}{3}$$

Question 13:

Using the method of integration find the area of the triangle ABC, coordinates of whose vertices are A(2,0), B(4,5) and C(6,3).





Equation of AB is

$$y-0 = \frac{5-0}{4-2}(x-2)$$
$$2y = 5x-10$$
$$y = \frac{5}{2}(x-2)$$

Equation of BC is

$$y-5 = \frac{3-5}{6-4}(x-4)$$

$$2y-10 = -2x+8$$

$$2y = -2x+18$$

$$y = -x+9$$

Equation of CA is

$$y-3 = \frac{0-3}{2-6}(x-6)$$

$$-4y+12 = -3x+18$$

$$4y = 3x-6$$

$$y = \frac{3}{4}(x-2)$$



$$ar(\Delta ABC) = ar(ABLA) + ar(BLMCB) - ar(ACMA)$$

$$= \int_{2}^{4} \frac{5}{2}(x-2) dx + \int_{4}^{6} (-x+9) dx - \int_{2}^{6} \frac{3}{4}(x-2) dx$$

$$= \frac{5}{2} \left[\frac{x^{2}}{2} - 2x \right]_{2}^{4} + \left[\frac{-x^{2}}{2} + 9x \right]_{4}^{6} - \frac{3}{4} \left[\frac{x^{2}}{2} - 2x \right]_{2}^{6}$$

$$= \frac{5}{2} [8 - 8 - 2 + 4] + [-18 + 54 + 8 - 36] - \frac{3}{4} [18 - 12 - 2 + 4]$$

$$= 5 + 8 - \frac{3}{4} (8)$$

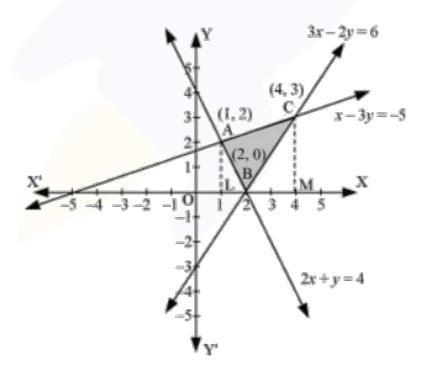
$$= 13 - 6$$

$$= 7 units.$$

Question 14:

Using the method of integration find the area of the region bounded by lines: 2x + y = 4, 3x - 2y = 6 and x - 3y + 5 = 0.

Solution:



AL and CM are perpendicular on x-axis.



$$ar(\Delta ABC) = ar(ALMCA) - ar(ALB) - ar(CMB)$$

$$= \int_{1}^{4} \left(\frac{x+5}{3}dx\right) - \int_{1}^{2} (4-2x)dx - \int_{2}^{4} \left(\frac{3x-6}{2}\right)dx$$

$$= \frac{1}{3} \left[\frac{x^{2}}{2} + 5x\right]_{1}^{4} - \left[4x - x^{2}\right]_{1}^{2} - \frac{1}{2} \left[\frac{3x^{2}}{2} - 6x\right]_{2}^{4}$$

$$= \frac{1}{3} \left[8 + 20 - \frac{1}{2} - 5\right] - \left[8 - 4 - 4 + 1\right] - \frac{1}{2} \left[24 - 24 - 6 + 12\right]$$

$$= \left(\frac{1}{3} \times \frac{45}{2}\right) - (1) - \frac{1}{2}(6)$$

$$= \frac{15}{2} - 1 - 3$$

$$= \frac{15}{2} - 4$$

$$= \frac{15 - 8}{2}$$

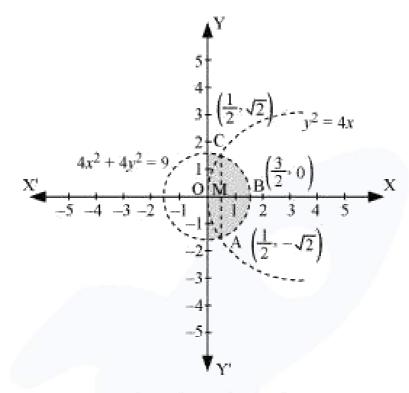
$$= \frac{7}{2}$$



Question 15:

Find the area of the region $\{(x,y): y^2 \le 4x, 4x^2 + 4y^2 \le 9\}$

Solution:



Points of intersection of curves are $\left(\frac{1}{2}, \sqrt{2}\right)$ and $\left(\frac{1}{2}, -\sqrt{2}\right)$.

Required area is OABCO.

Area OABCO is symmetrical about *x*-axis.

$$Area\ OABCO\ =\ 2\times Area\ OBC$$

$$ar(OBCO) = ar(OMC) + ar(MBC)$$

$$= \int_0^{\frac{1}{2}} 2\sqrt{x} dx + \int_{\frac{1}{2}}^{\frac{3}{2}} \frac{1}{2} \sqrt{9 - 4x^2} dx$$

$$= \int_0^{\frac{1}{2}} 2\sqrt{x} dx + \int_{\frac{1}{2}}^{\frac{3}{2}} \frac{1}{2} \sqrt{(3)^2 - (2x)^2} dx$$



$$put \ 2x = t \Rightarrow dx = \frac{dt}{2}$$

$$When \ x = \frac{3}{2}, t = 3 \ and \ when \ x = \frac{1}{2}, t = 1$$

$$ar(OBCO) = \int_0^{\frac{1}{2}} 2\sqrt{x} dx + \frac{1}{4} \int_1^3 \sqrt{(3)^2 - (t)^2} dt$$

$$= 2 \left[\frac{x^{\frac{3}{2}}}{\frac{3}{2}} \right]_0^{\frac{1}{2}} + \frac{1}{4} \left[\frac{t}{2} \sqrt{9 - t^2} + \frac{9}{2} \sin^{-1} \left(\frac{t}{3} \right) \right]_1^3$$

$$= 2 \left[\frac{2}{3} \left(\frac{1}{2} \right)^{\frac{3}{2}} \right] + \frac{1}{4} \left[\left\{ \frac{3}{2} \sqrt{9 - (3)^2} + \frac{9}{2} \sin^{-1} \left(\frac{3}{3} \right) \right\} - \left\{ \frac{1}{2} \sqrt{9 - (1)^2} + \frac{9}{2} \sin^{-1} \left(\frac{1}{3} \right) \right\} \right]$$

$$= \frac{2}{3\sqrt{2}} + \frac{1}{4} \left[\left\{ 0 + \frac{9}{2} \sin^{-1} (1) \right\} - \left\{ \frac{1}{2} \sqrt{8} + \frac{9}{2} \sin^{-1} \left(\frac{1}{3} \right) \right\} \right]$$

$$= \frac{\sqrt{2}}{3} + \frac{1}{4} \left[\frac{9\pi}{4} - \sqrt{2} - \frac{9}{2} \sin^{-1} \left(\frac{1}{3} \right) \right]$$

$$= \frac{\sqrt{2}}{3} + \frac{9\pi}{16} - \sqrt{2} - \frac{9}{8} \sin^{-1} \left(\frac{1}{3} \right)$$

$$= \frac{9\pi}{16} - \frac{9}{8} \sin^{-1} \left(\frac{1}{3} \right) + \frac{\sqrt{2}}{12}$$

$$ar(OABCO) = 2 \times ar(OBC)$$

$$= 2 \times \frac{9\pi}{16} - \frac{9}{8} \sin^{-1} \left(\frac{1}{3}\right) + \frac{\sqrt{2}}{12}$$

$$= \frac{9\pi}{8} - \frac{9}{4} \sin^{-1} \left(\frac{1}{3}\right) + \frac{\sqrt{2}}{6}$$

$$= \frac{9\pi}{8} - \frac{9}{4} \sin^{-1} \left(\frac{1}{3}\right) + \frac{1}{3\sqrt{2}}$$

Question 16:

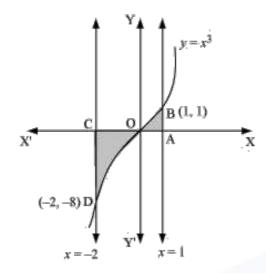
Area bounded by the curve $y = x^3$, the x-axis and the coordinates x = -2 and x = 1 is

(B)
$$-\frac{15}{4}$$

(C)
$$\frac{15}{4}$$

(D)
$$\frac{17}{4}$$





required area =
$$\int_{-2}^{0} y dx + \int_{0}^{1} y dx$$

= $\int_{-2}^{0} x^{3} dx + \int_{0}^{1} x^{3} dx$
= $\left[\frac{x^{4}}{4}\right]_{-2}^{0} + \left[\frac{x^{4}}{4}\right]_{0}^{1}$
= $\left[\frac{(-2)^{4}}{4} + \frac{1}{4}\right]$
= $\left(4 + \frac{1}{4}\right) = \frac{17}{4}$

Correct answer is D

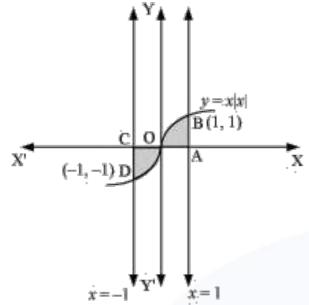
Question17:

The area bounded by the curve y = x|x|, x-axis and the coordinates x = -1 and x = 1 is given by

[Hint: $y = x^2$ if x > 0 and $y = -x^2$ if x < 0]

- (A) 0
- (B) $\frac{1}{3}$
- (C) $\frac{2}{3}$
- (D) $\frac{4}{3}$





required area
$$= \int_{-1}^{1} y dx$$

$$= \int_{-1}^{1} x |x| dx$$

$$= \int_{-1}^{0} x^{2} dx + \int_{0}^{1} x^{2} dx$$

$$= \left[\frac{x^{3}}{3} \right]_{-1}^{0} + \left[\frac{x^{3}}{3} \right]_{0}^{1}$$

$$= -\left(-\frac{1}{3} \right) + \frac{1}{3}$$

$$= \frac{2}{3}$$

Correct answer is C.

Question 18:

The area of the circle $x^2 + y^2 = 16$ exterior to the parabola $y^2 = 6x$.

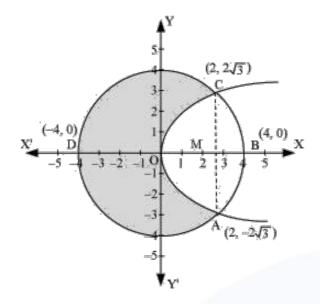
(A)
$$\frac{4}{3} (4\pi - \sqrt{3})$$

(B)
$$\frac{4}{3} (4\pi + \sqrt{3})$$

(C)
$$\frac{4}{3} (8\pi - \sqrt{3})$$

(A)
$$\frac{4}{3} \left(4\pi - \sqrt{3} \right)$$
 (B) $\frac{4}{3} \left(4\pi + \sqrt{3} \right)$ (C) $\frac{4}{3} \left(8\pi - \sqrt{3} \right)$ (D) $\frac{4}{3} \left(8\pi + \sqrt{3} \right)$





Required area = 2[Area (OADO) + Area (ADBA)]

$$2[ar(OADO) + ar(ADBA)] = 2\left[\int_{0}^{2} \sqrt{6x} dx + \int_{2}^{4} \sqrt{16 - x^{2}} dx\right]$$

$$= 2\int_{0}^{2} \sqrt{6x} dx + 2\int_{2}^{4} \sqrt{16 - x^{2}} dx$$

$$= 2\sqrt{6}\int_{0}^{2} \sqrt{x} dx + 2\int_{2}^{4} \sqrt{16 - x^{2}} dx$$

$$= 2\sqrt{6} \times \frac{2}{3} \left[\frac{x^{\frac{3}{2}}}{x^{\frac{3}{2}}}\right]_{0}^{2} + 2\left[\frac{x}{2}\sqrt{16 - x^{2}} + \frac{16}{2}\sin^{-1}\left(\frac{x}{4}\right)\right]_{2}^{4}$$

$$= \frac{4\sqrt{6}}{3}\left(2\sqrt{2} - 0\right) + 2\left[\left\{0 + 8\sin^{-1}\left(1\right)\right\} - \left\{2\sqrt{3} + 8\sin^{-1}\left(\frac{1}{2}\right)\right\}\right]$$

$$= \frac{16\sqrt{3}}{3} + 2\left[8 \times \frac{\pi}{2} - 2\sqrt{3} - 8 \times \frac{\pi}{6}\right]$$

$$= \frac{16\sqrt{3}}{3} + 8\pi - 4\sqrt{3} - \frac{8\pi}{3}$$

$$= \frac{16\sqrt{3} + 24\pi - 12\sqrt{3} - 8\pi}{3}$$

$$= \frac{4\sqrt{3} + 16\pi}{3}$$

$$= \frac{4}{3}\left[4\pi + \sqrt{3}\right] \text{ units}$$



Area of circle
$$=\pi (r)^2$$

 $=\pi (4)^2$
 $=16\pi$
required area $=16\pi - \frac{4}{3} \left[4\pi + \sqrt{3} \right]$
 $=\frac{4}{3} \left[4 \times 3\pi - 4\pi - \sqrt{3} \right]$
 $=\frac{4}{3} \left(8\pi - \sqrt{3} \right)$

Correct answer is C.

Question 19:

The area bounded by the y-axis, $y = \cos x$ and $y = \sin x$ when $0 \le x \le \frac{\pi}{2}$.

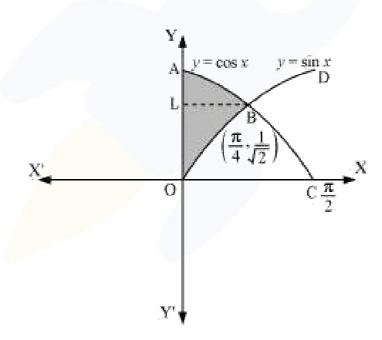
(A)
$$2(\sqrt{2}-1)$$

(B) $\sqrt{2} - 1$

(C) $\sqrt{2} + 1$

(D) $\sqrt{2}$

Solution:



Required area = Area (ABLA) + Area (OBLO)



$$ar(ABLA) + ar(OBLO) = \int_{\frac{1}{\sqrt{2}}}^{1} x dy + \int_{0}^{\frac{1}{\sqrt{2}}} x dy$$

$$= \int_{\frac{1}{\sqrt{2}}}^{1} \cos^{-1} y dy + \int_{0}^{\frac{1}{\sqrt{2}}} \sin^{-1} x dy$$

$$= \left[y \cos^{-1} y - \sqrt{1 - y^{2}} \right]_{\frac{1}{\sqrt{2}}}^{1} + \left[x \sin^{-1} x + \sqrt{1 - x^{2}} \right]_{0}^{\frac{1}{\sqrt{2}}}$$

$$= \left[\cos^{-1} (1) - \frac{1}{\sqrt{2}} \cos^{-1} \left(\frac{1}{\sqrt{2}} \right) + \sqrt{1 - \frac{1}{2}} \right] + \left[\frac{1}{\sqrt{2}} \sin^{-1} \left(\frac{1}{\sqrt{2}} \right) + \sqrt{1 - \frac{1}{2} - 1} \right]$$

$$= \frac{-\pi}{4\sqrt{2}} + \frac{1}{\sqrt{2}} + \frac{\pi}{4\sqrt{2}} + \frac{1}{\sqrt{2}} - 1$$

$$= \frac{2}{\sqrt{2}} - 1$$

$$= \sqrt{2} - 1$$

Correct answer is B.



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